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GB A 2148529

(58) Field of search

G2J

Selected US specifications from IPC sub-class G02B

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(54) Graded refractive index lens system

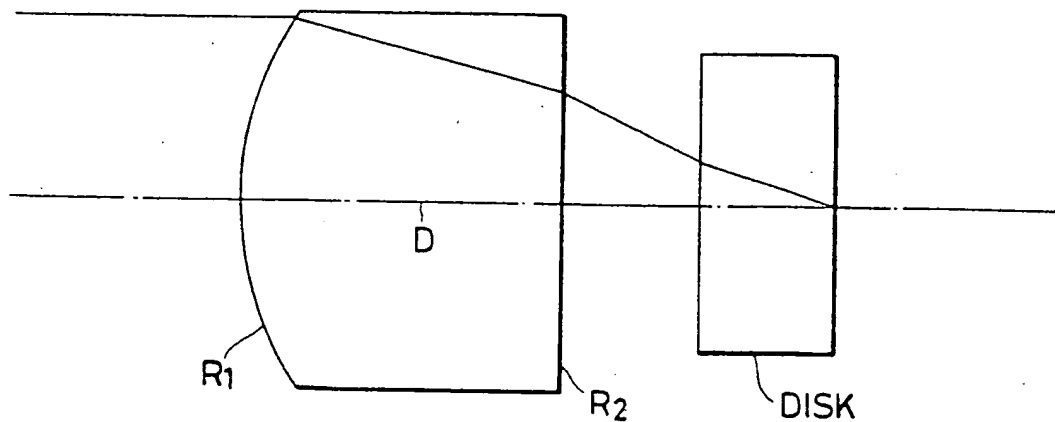
(57) A graded refractive index lens having at least one spherical surface and satisfying the equation

$$n^2 = n_0^2 (1 - (gr)^2 + h_4 (gr)^4 + h_6 (gr)^6 + \dots)$$

where n_0 = refractive index on optical axis and g, h are constants, selected to control aberrations.

The lens has particular application as an objective for optical video discs etc.

FIG. 1



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FIG. 1

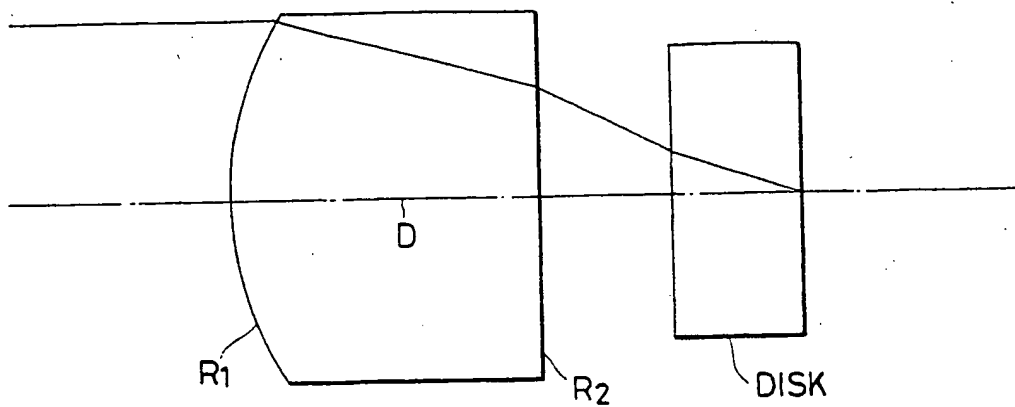


FIG. 2

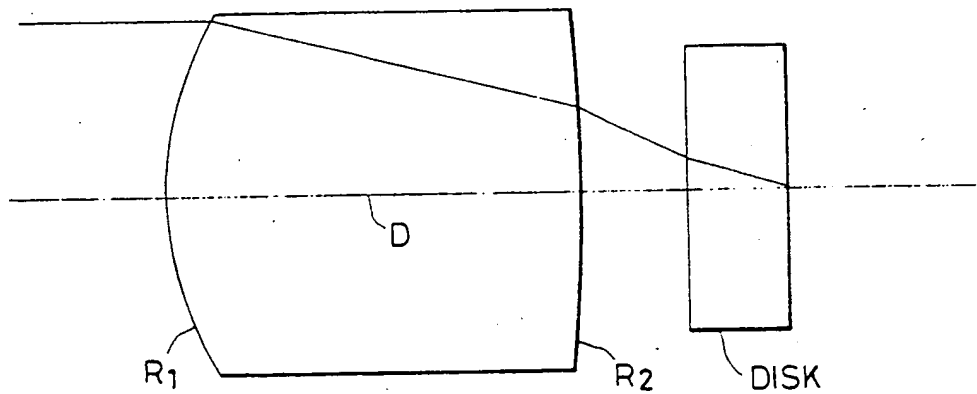


FIG. 3

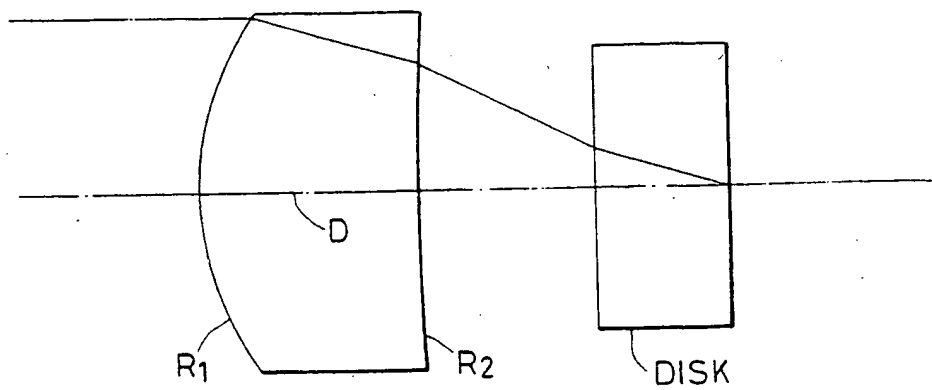


FIG. 4

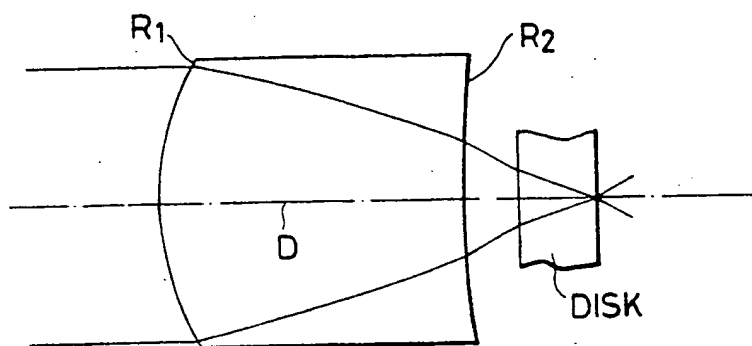


FIG. 5

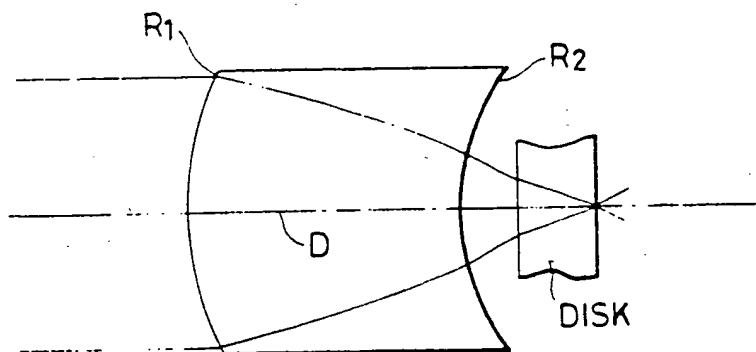


FIG. 6

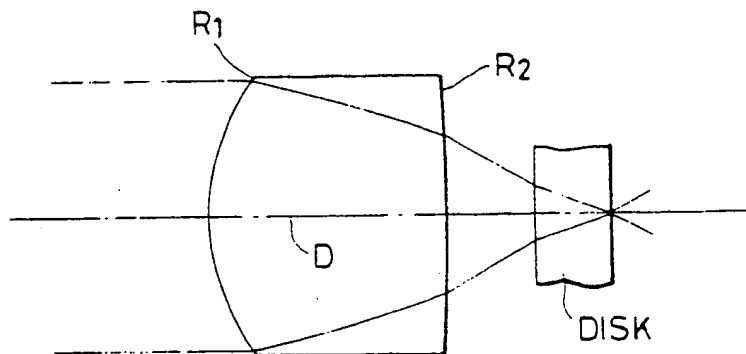


FIG. 7

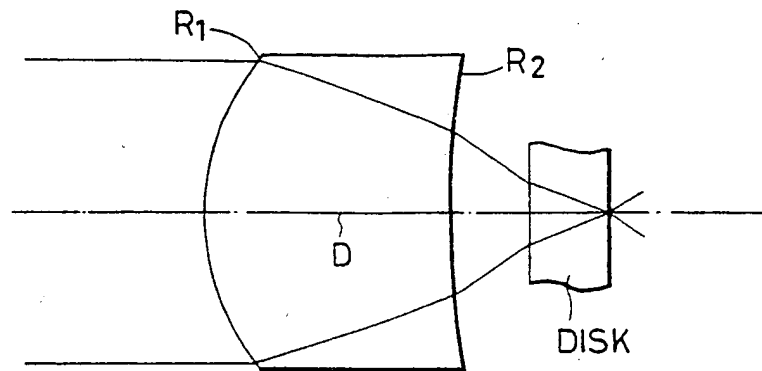


FIG. 8

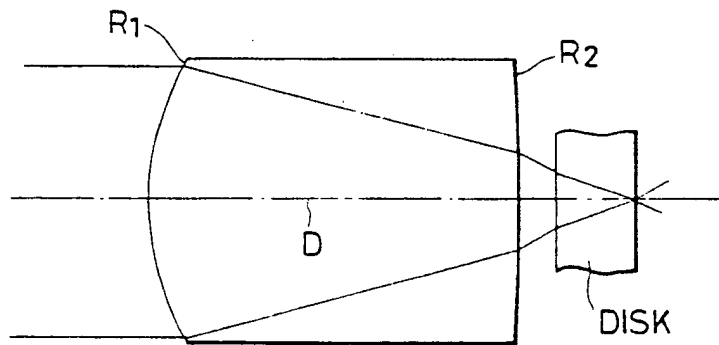


FIG. 9

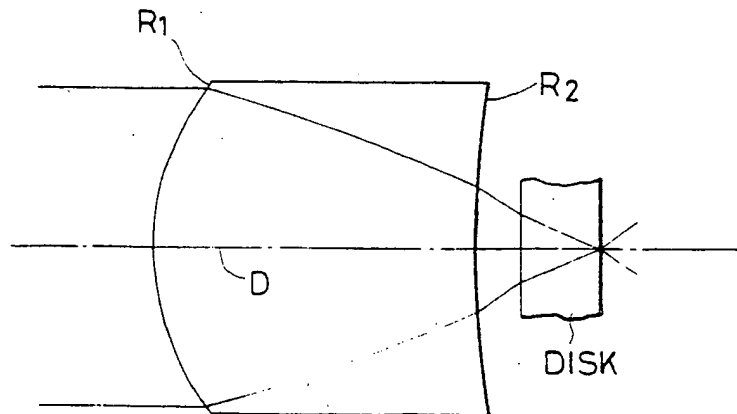


FIG. 10

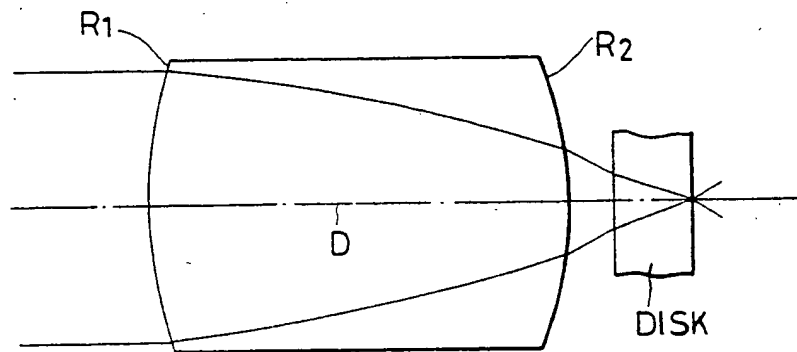


FIG. 11

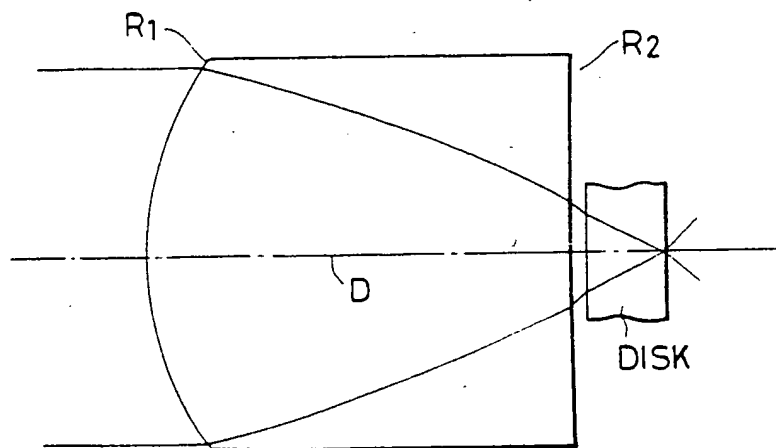


FIG. 12

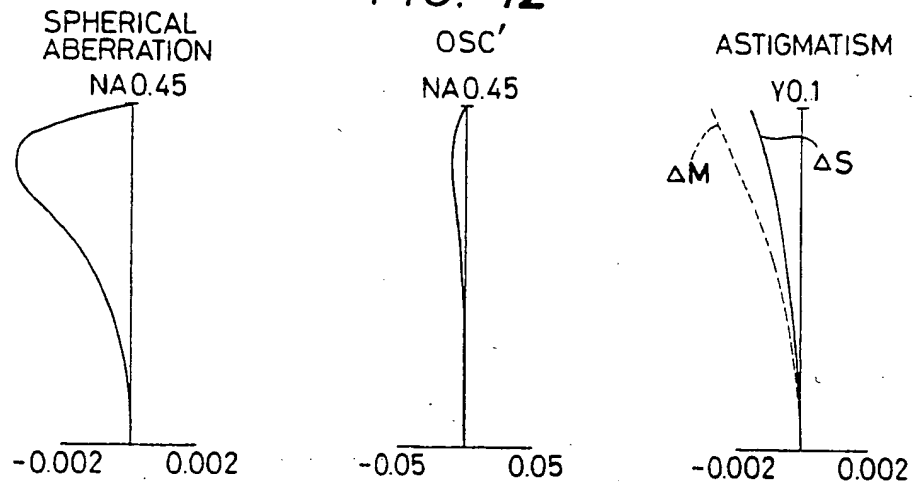


FIG. 13

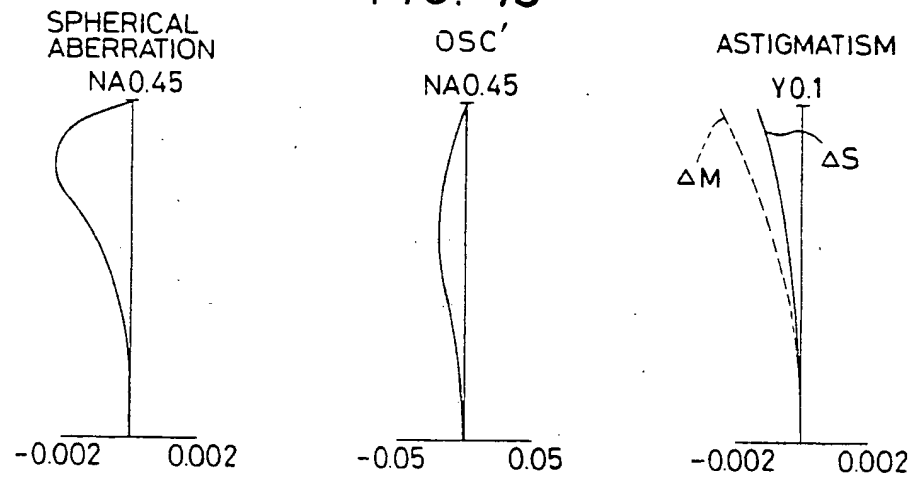


FIG. 14

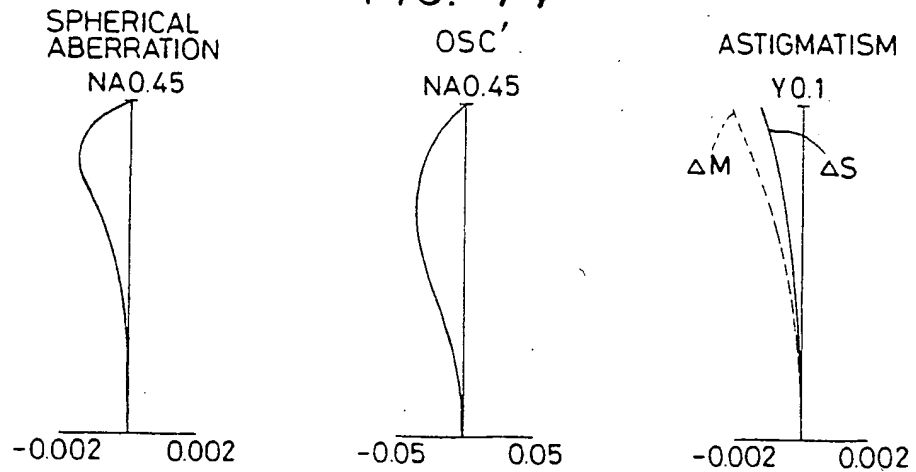


FIG. 15

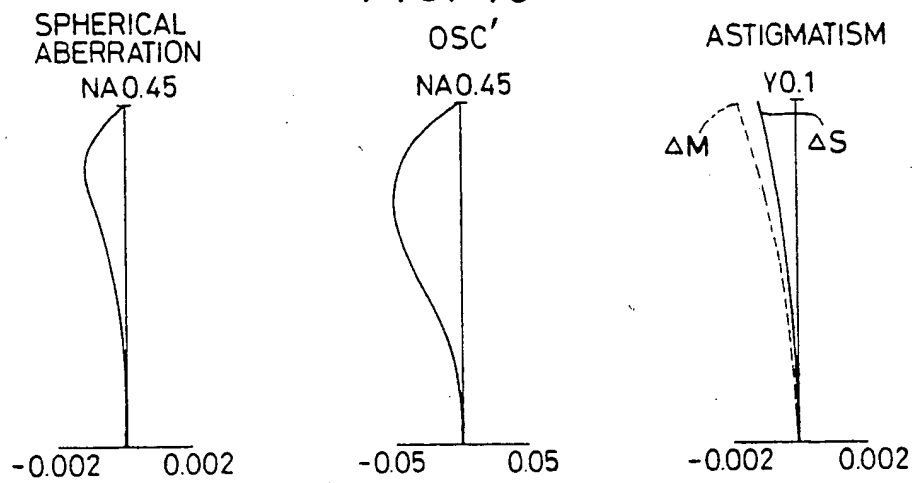


FIG. 16

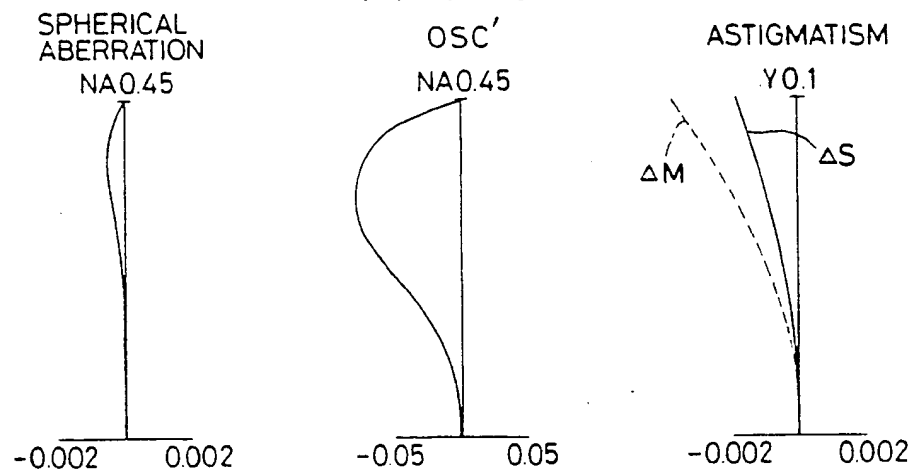
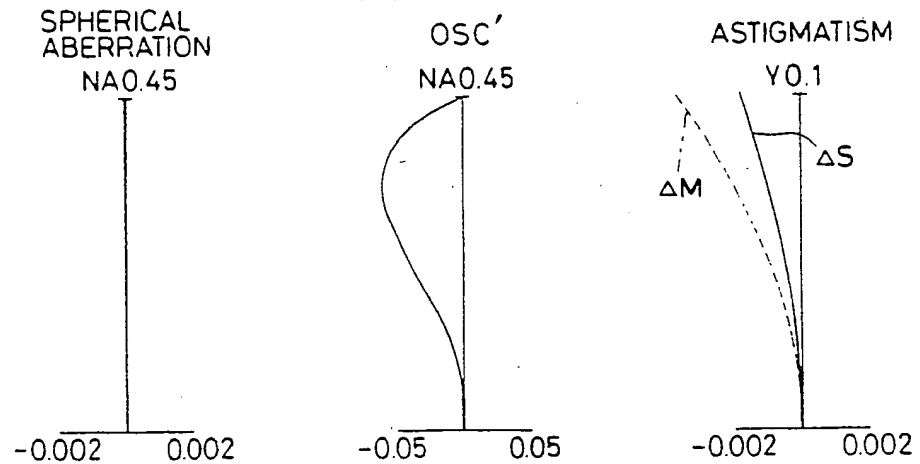


FIG. 17



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FIG. 18

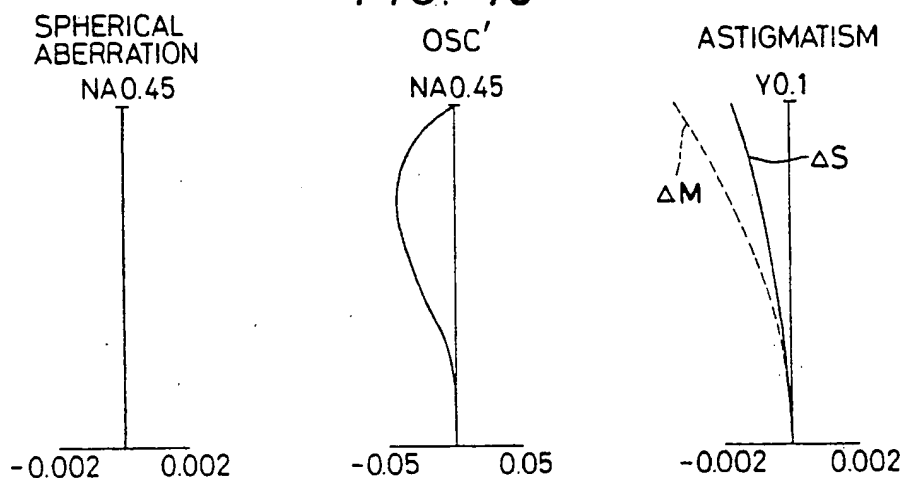


FIG. 19

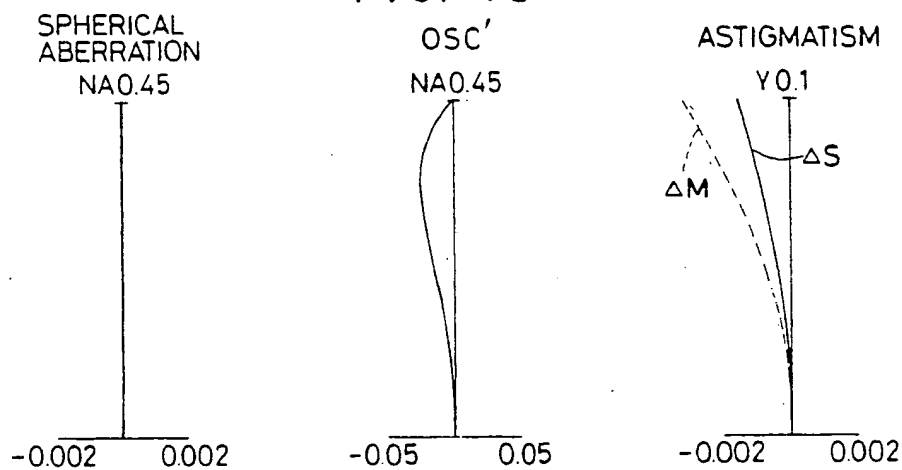


FIG. 20

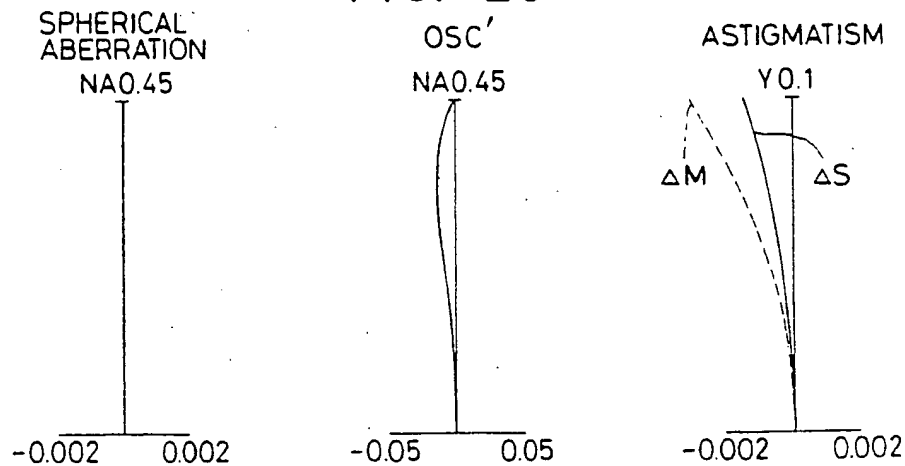


FIG. 21

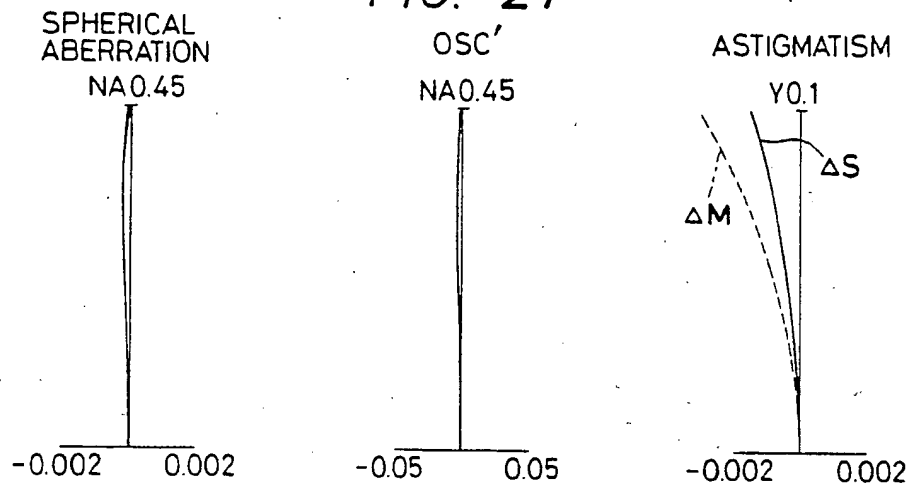


FIG. 22

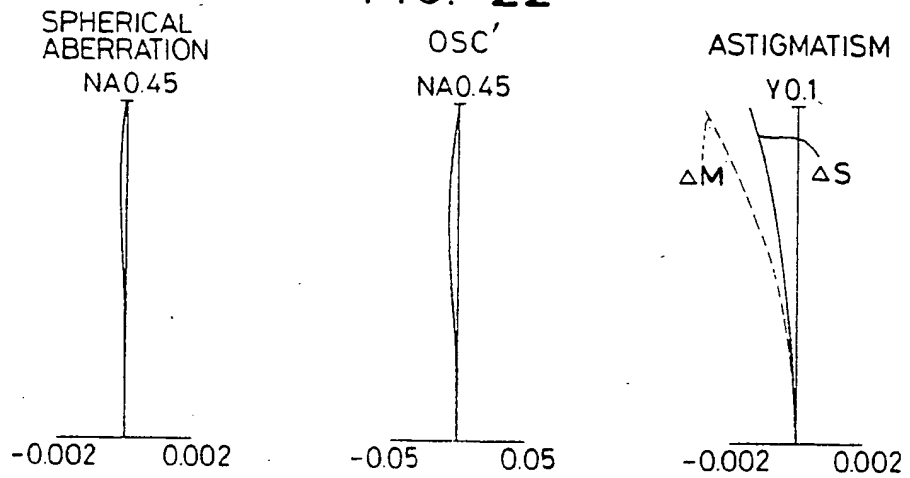


FIG. 23

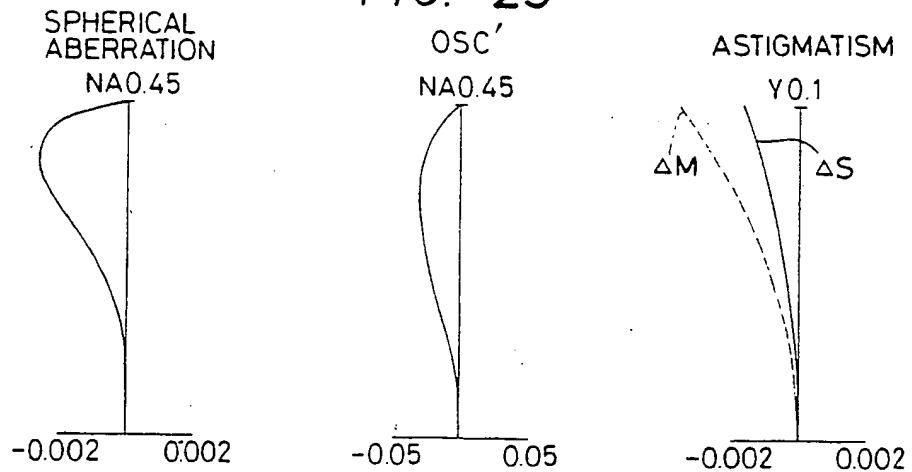


FIG. 24

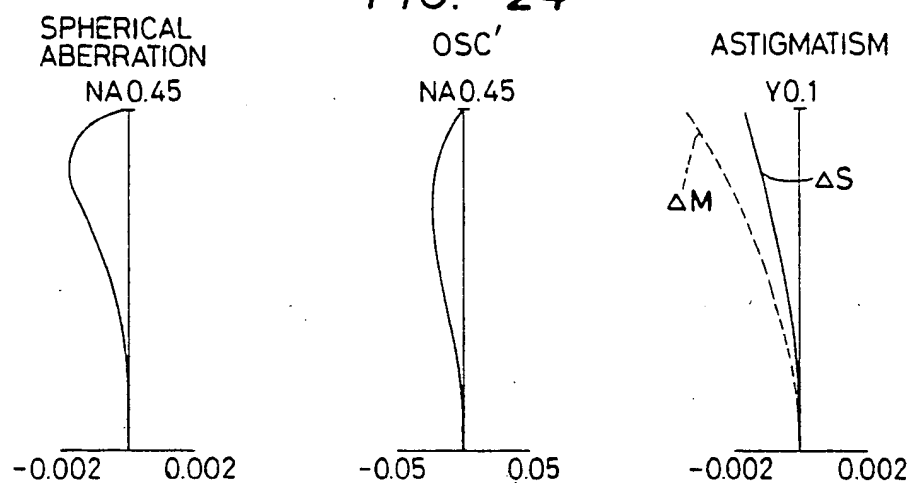


FIG. 25

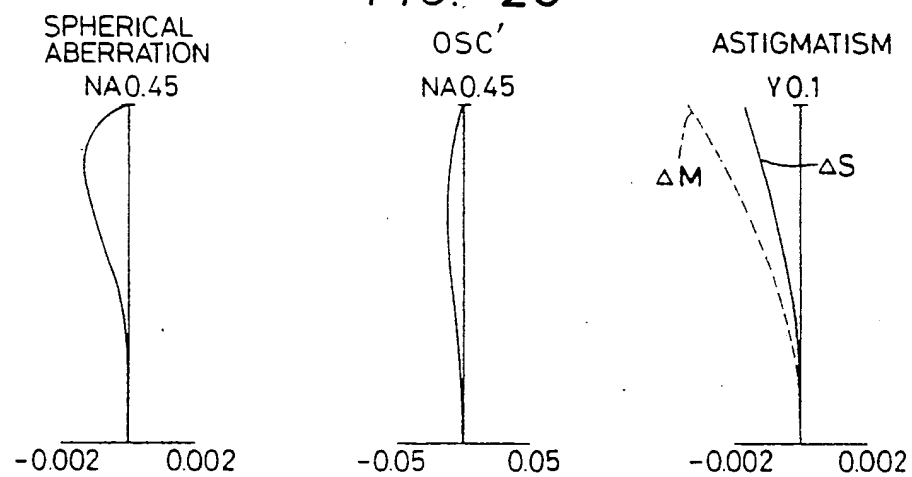
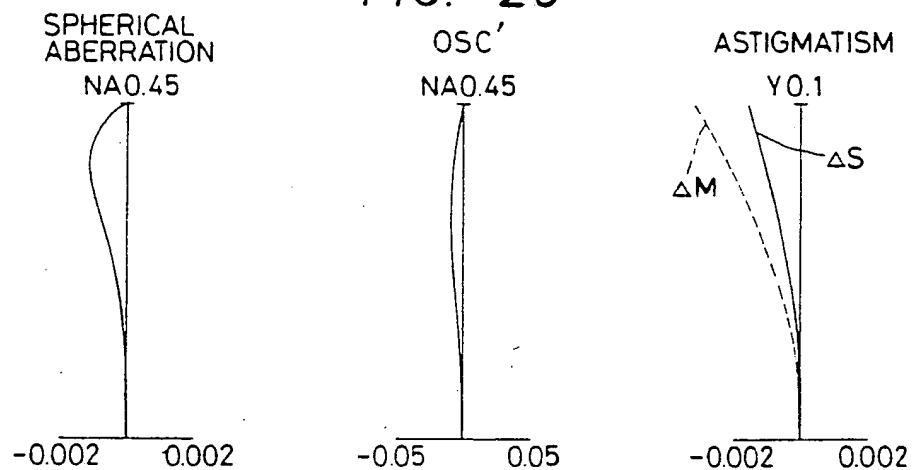


FIG. 26



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FIG. 27

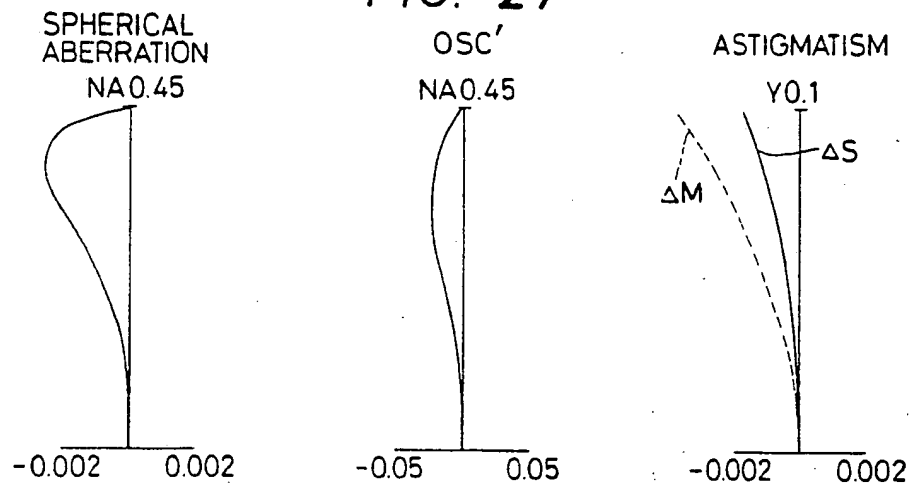


FIG. 28

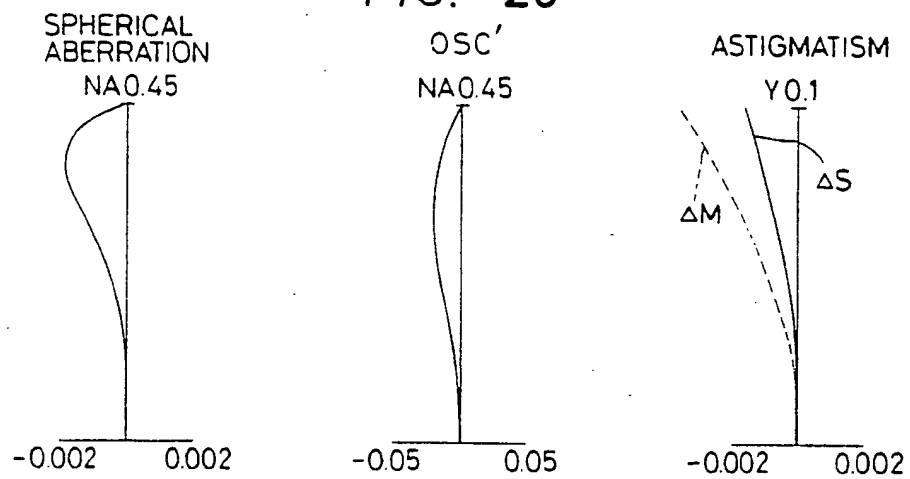


FIG. 29

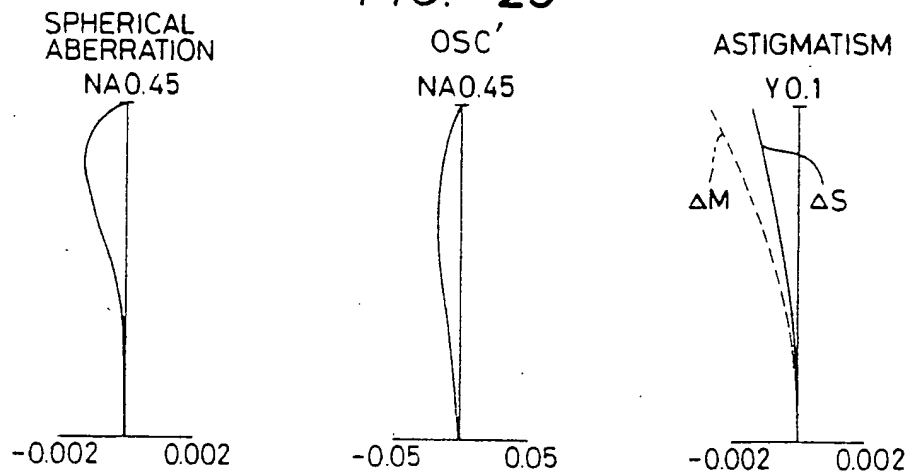


FIG. 30

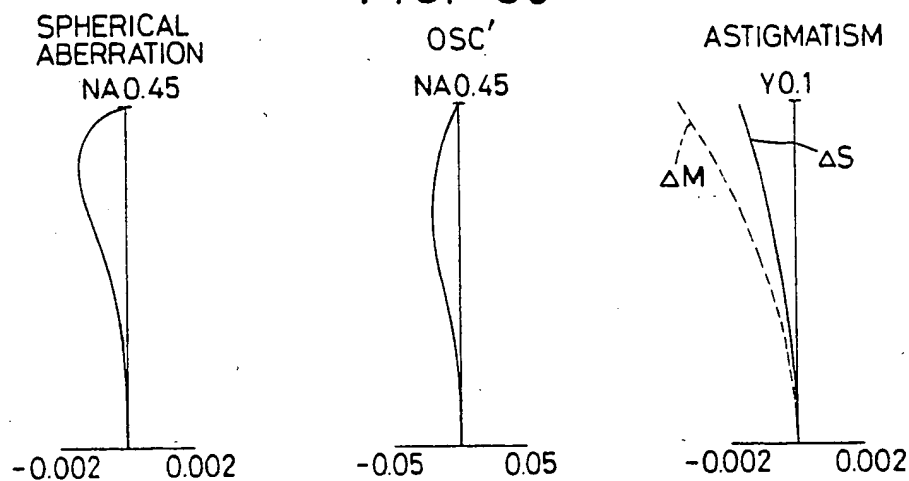


FIG. 31

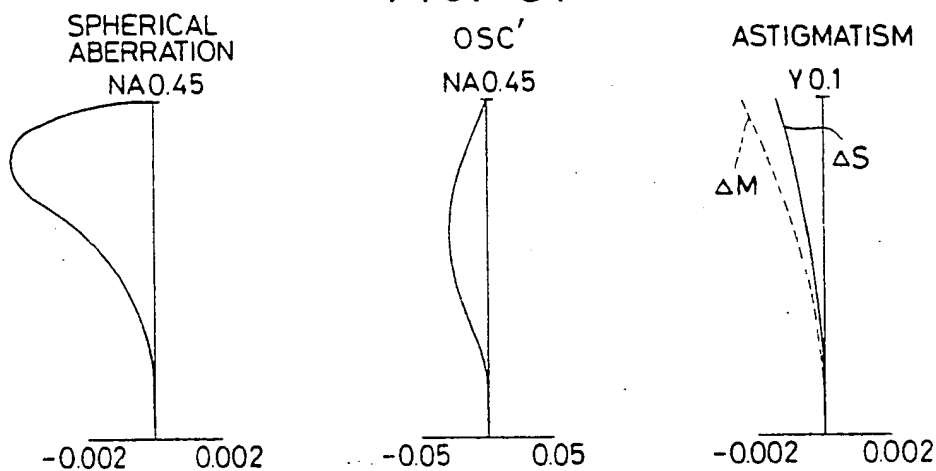


FIG. 32

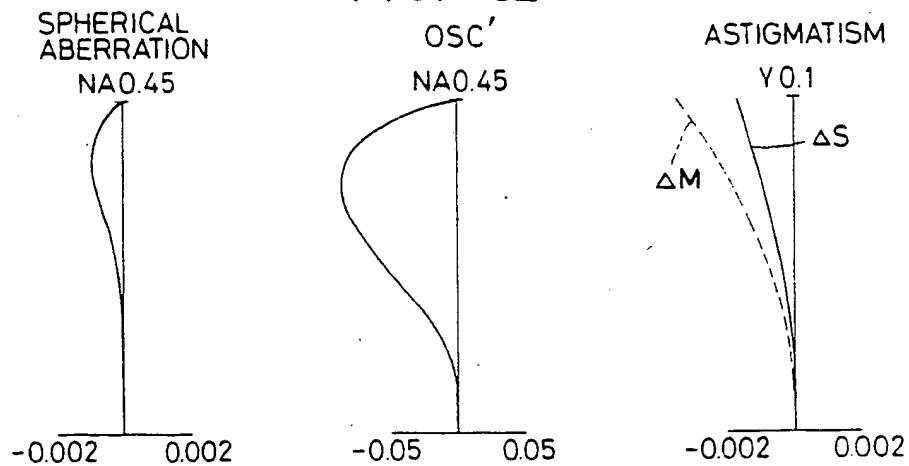


FIG. 33

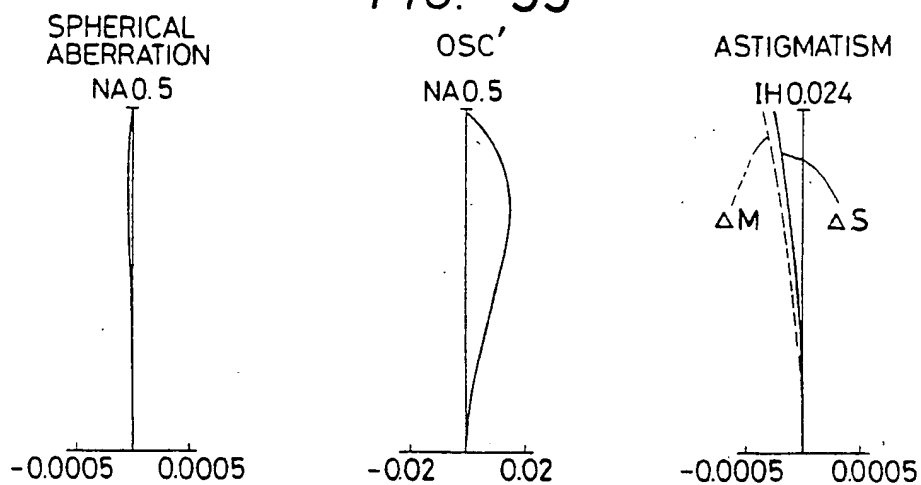


FIG. 34

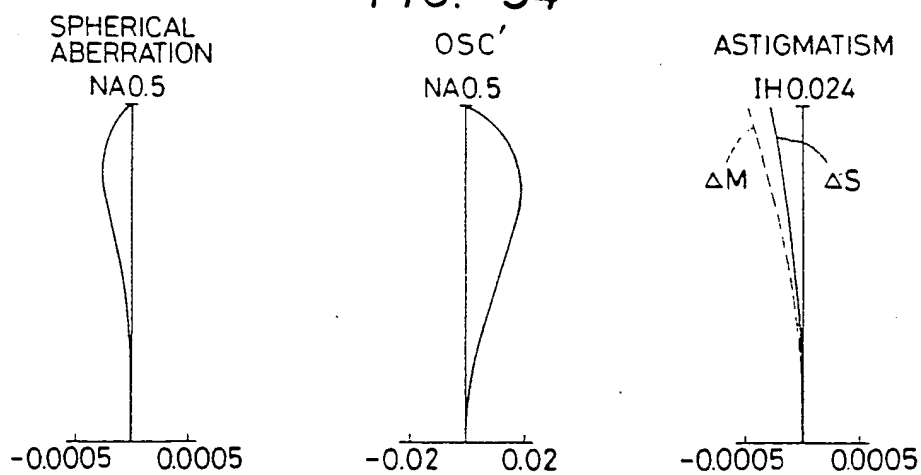


FIG. 35

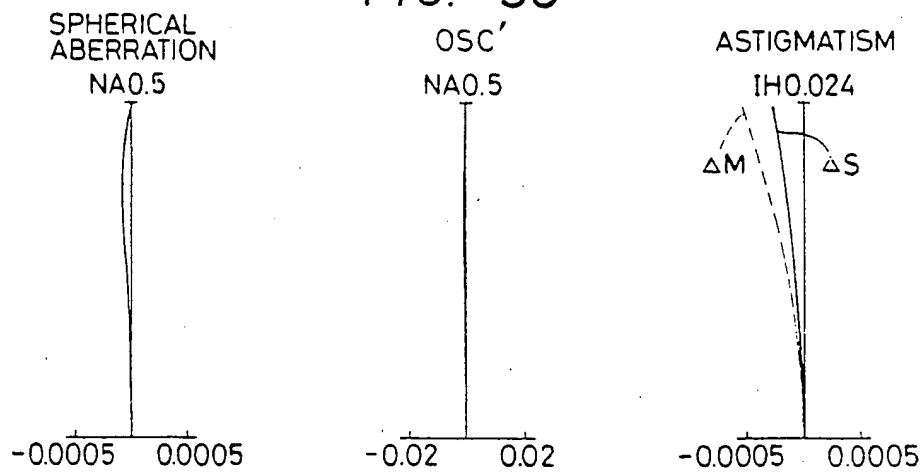


FIG. 36

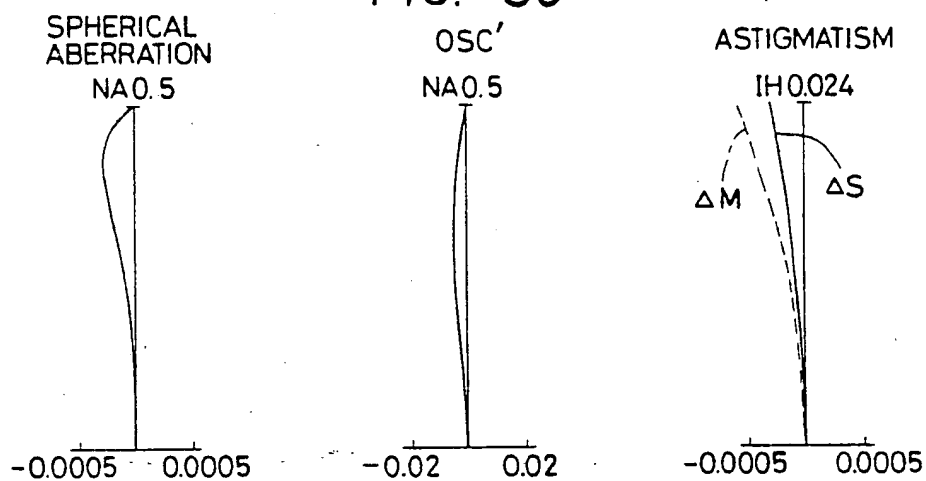


FIG. 37

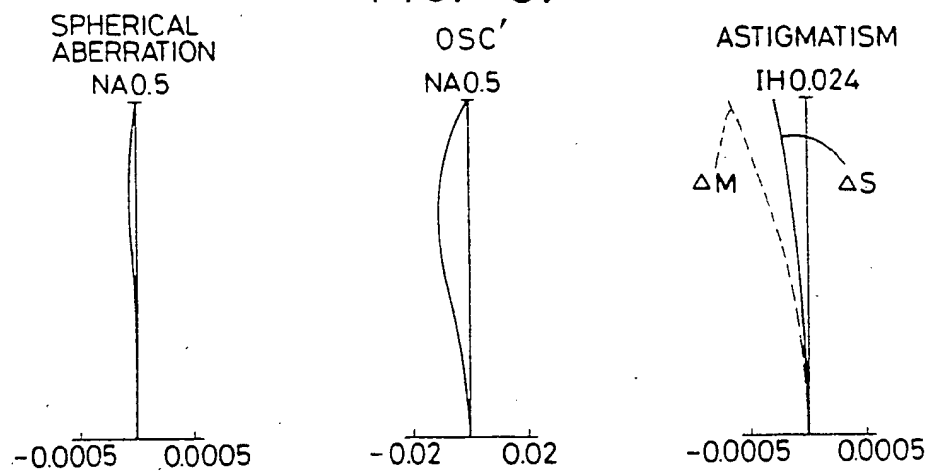


FIG. 38

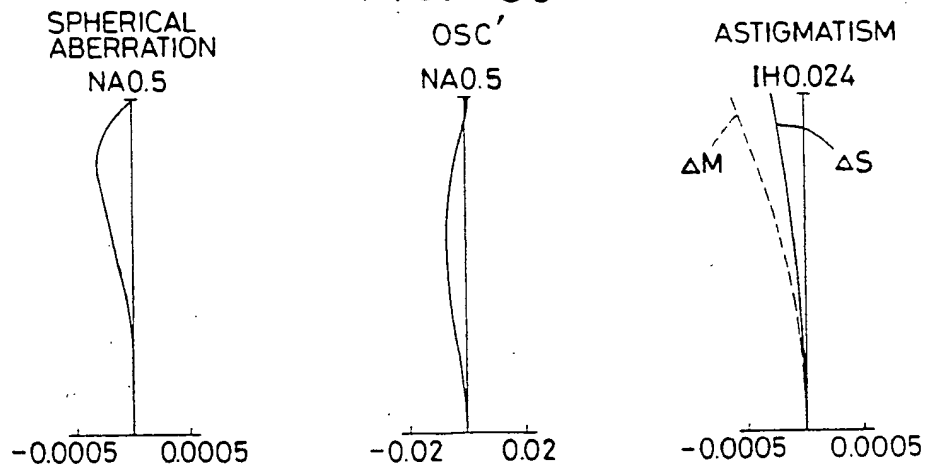


FIG. 39

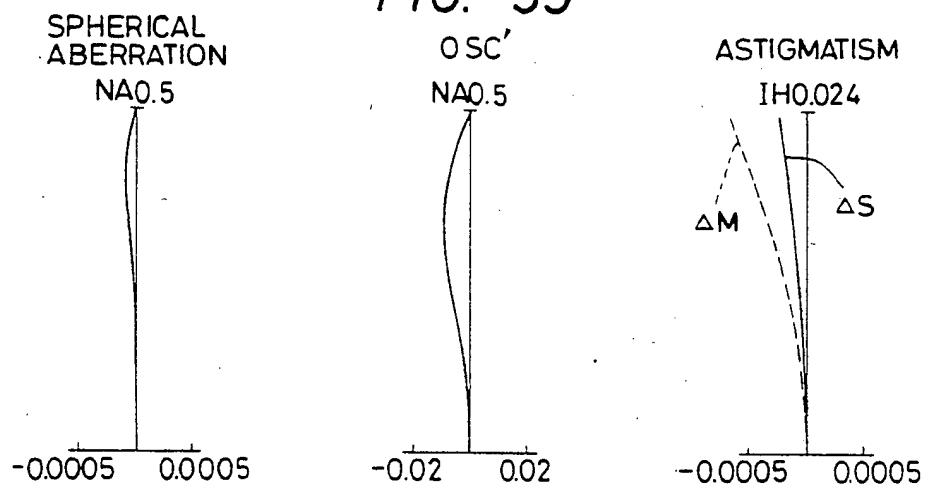


FIG. 40

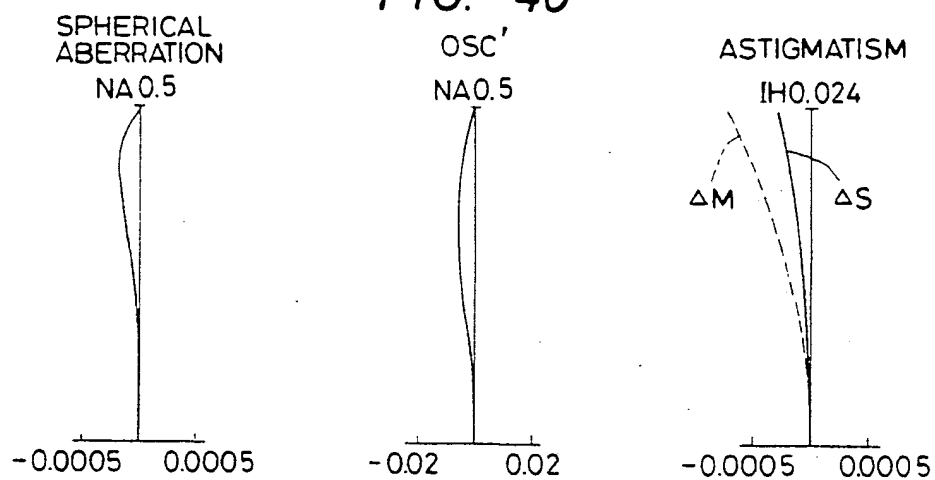


FIG. 41

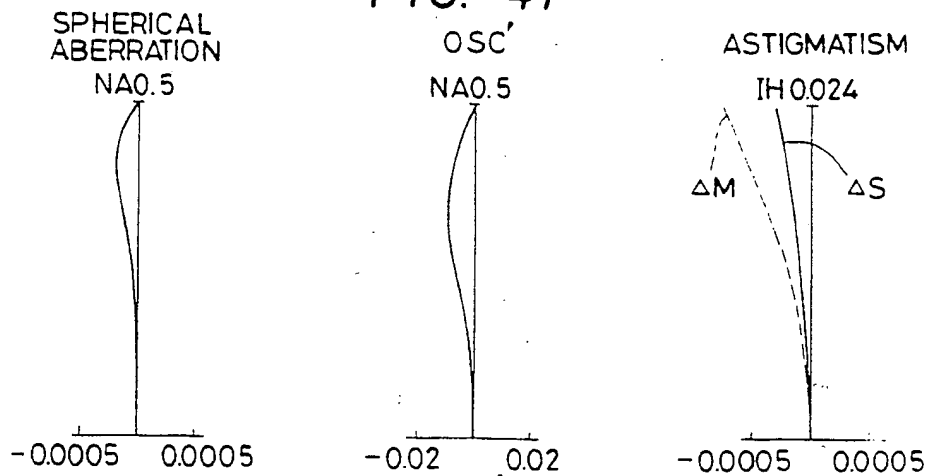


FIG. 42

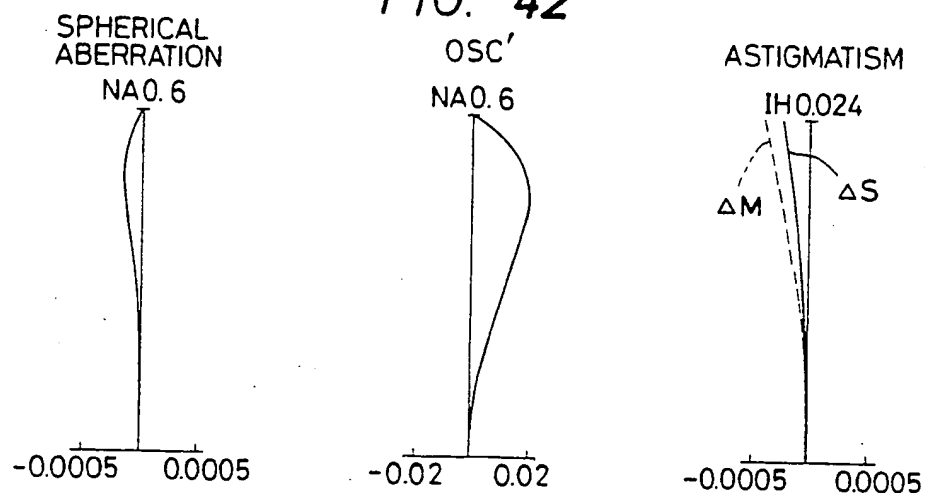


FIG. 43

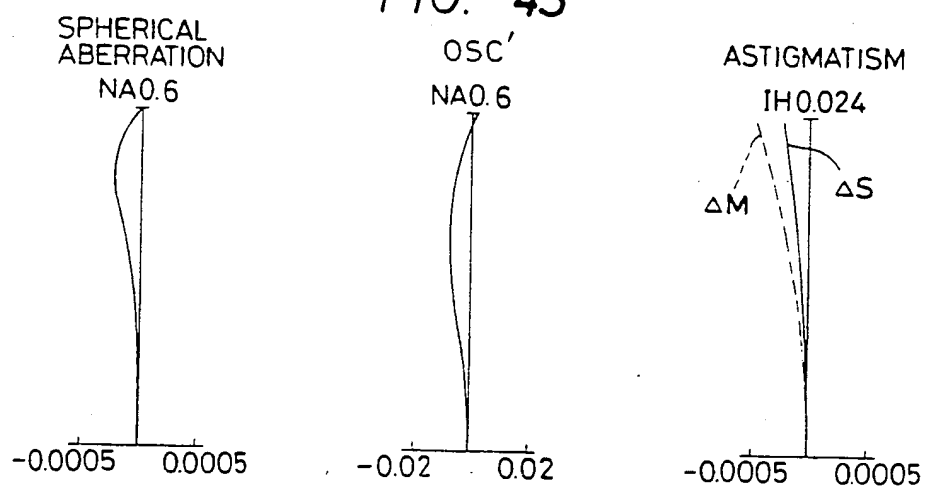


FIG. 44

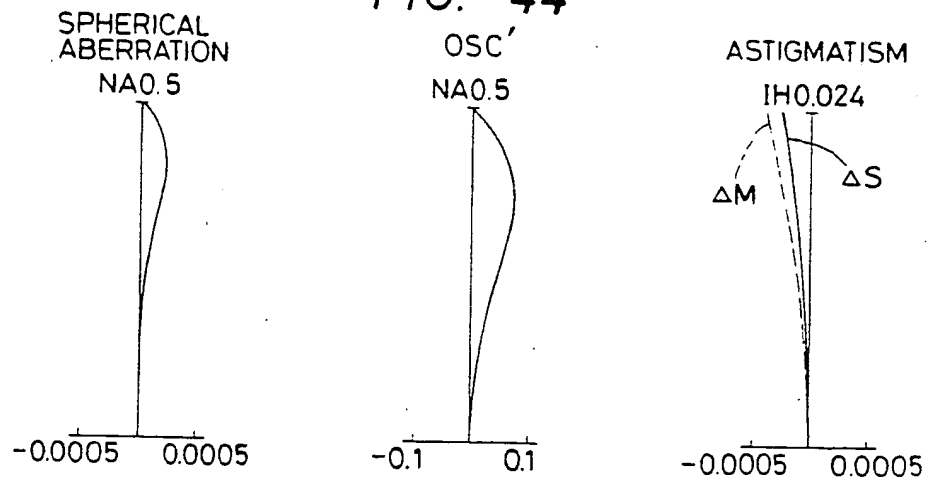


FIG. 45

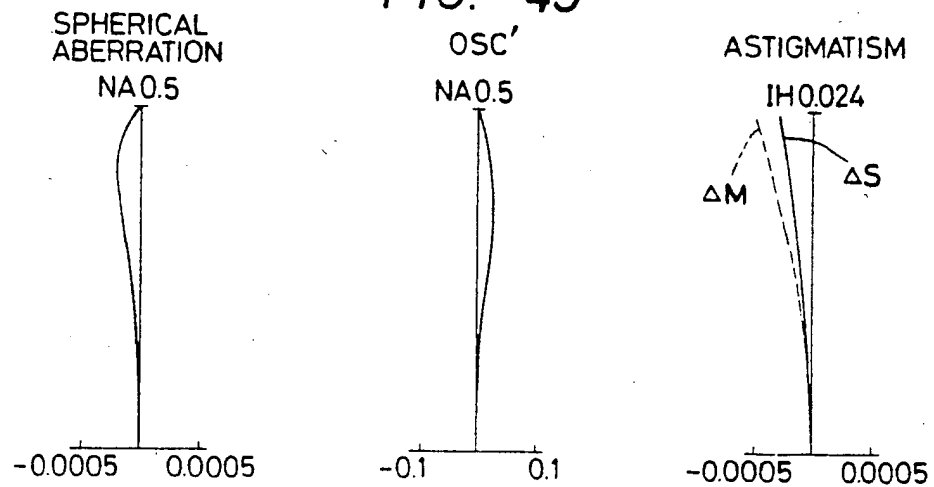


FIG. 46

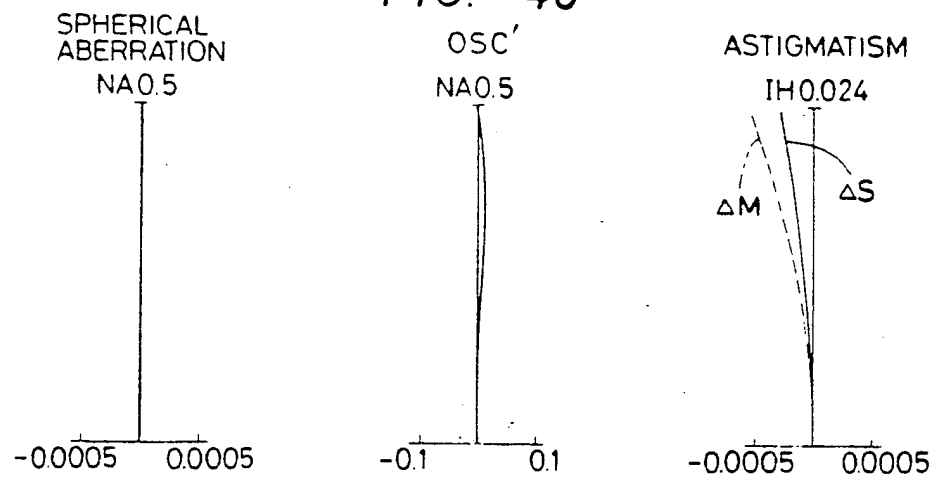


FIG. 47

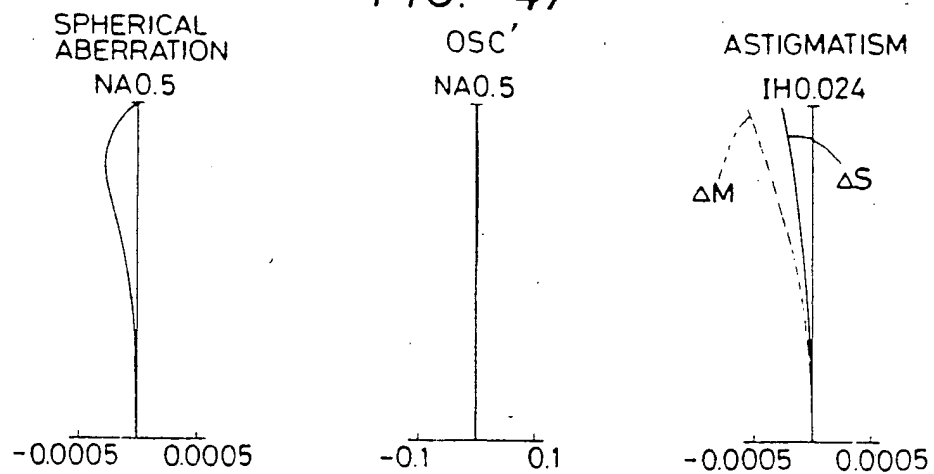


FIG. 48

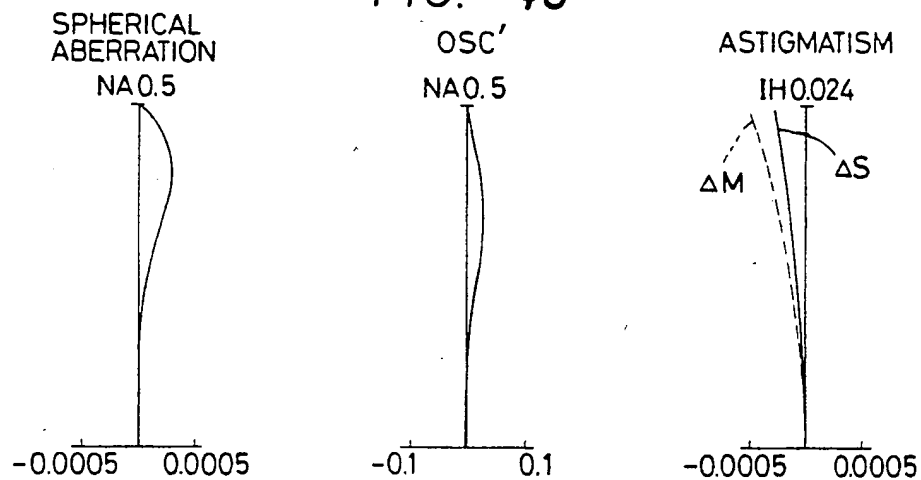


FIG. 49

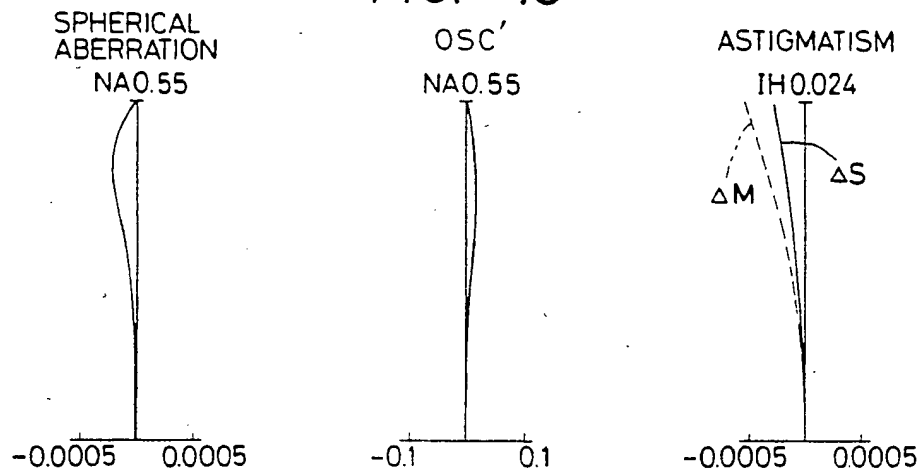
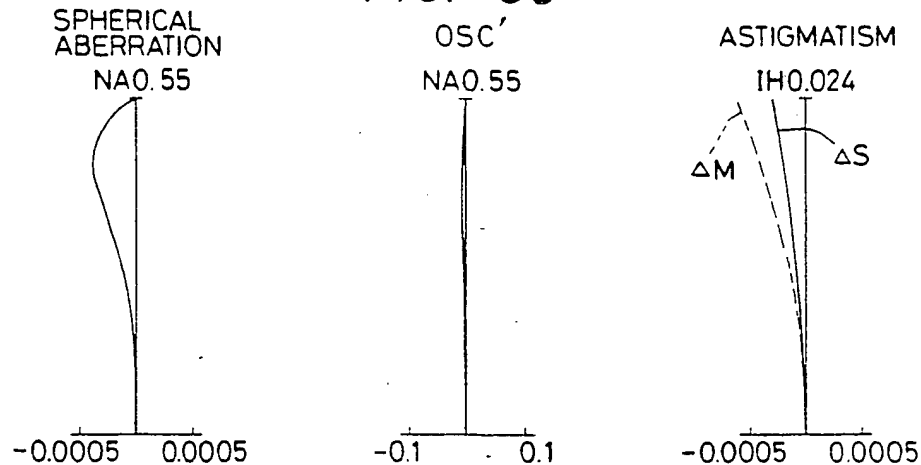


FIG. 50



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FIG. 51

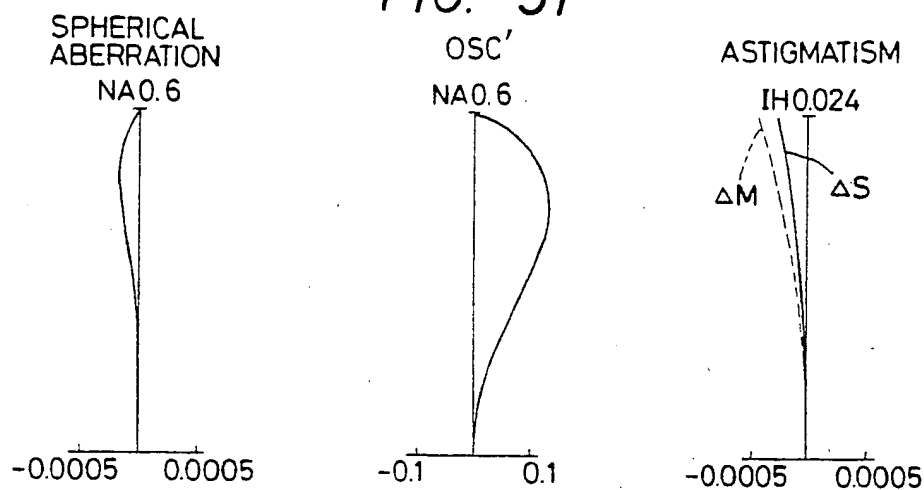


FIG. 52

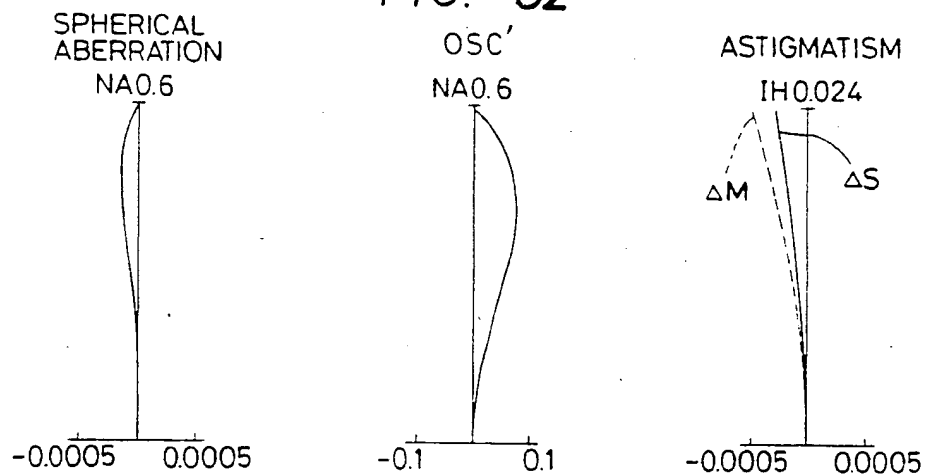
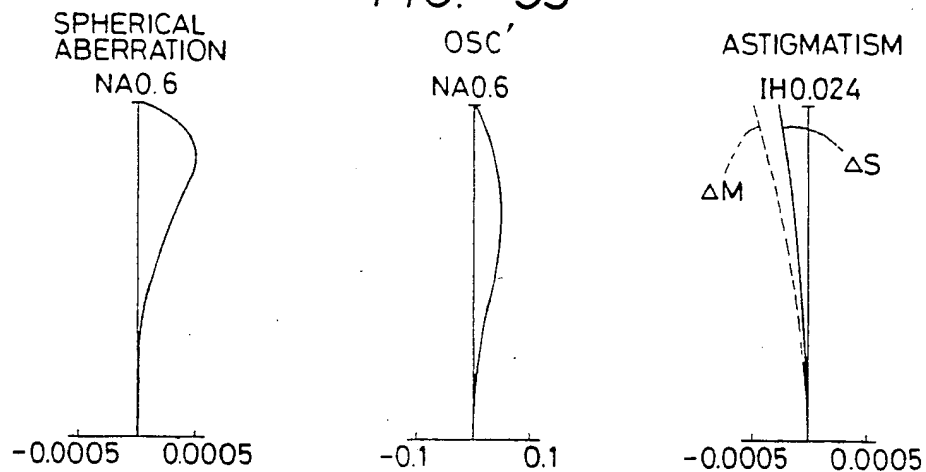


FIG. 53



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FIG. 54

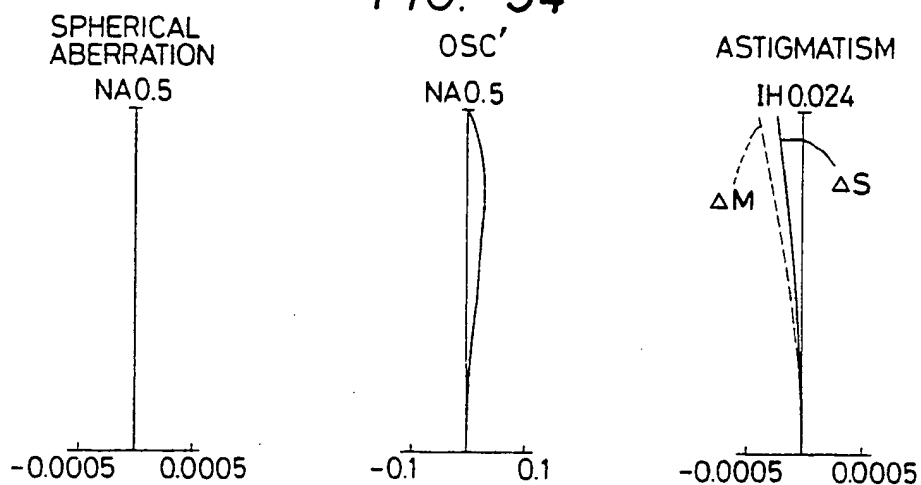


FIG. 55

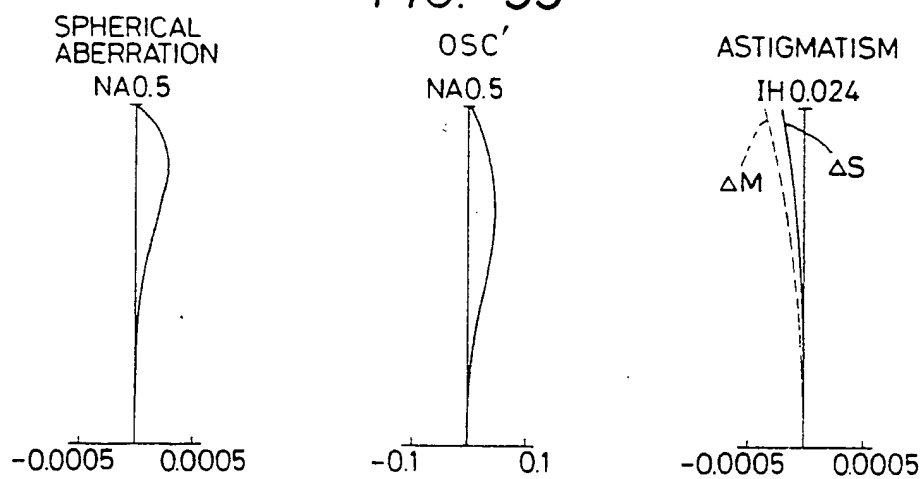


FIG. 56

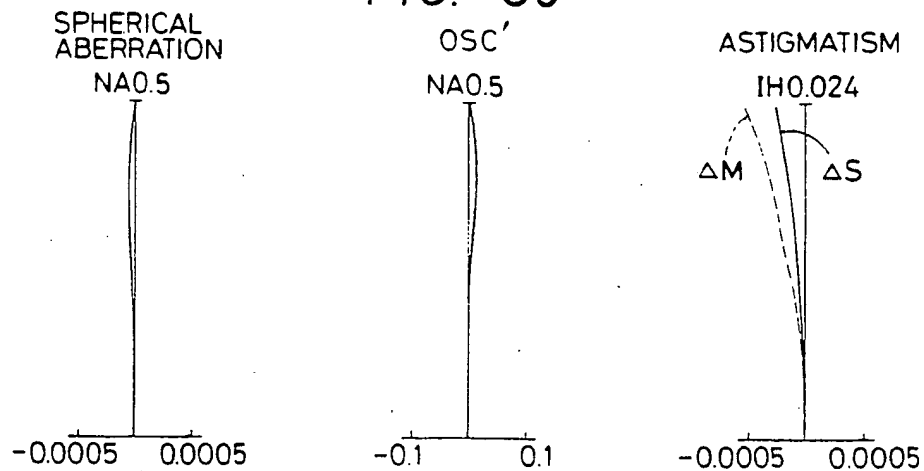


FIG. 57

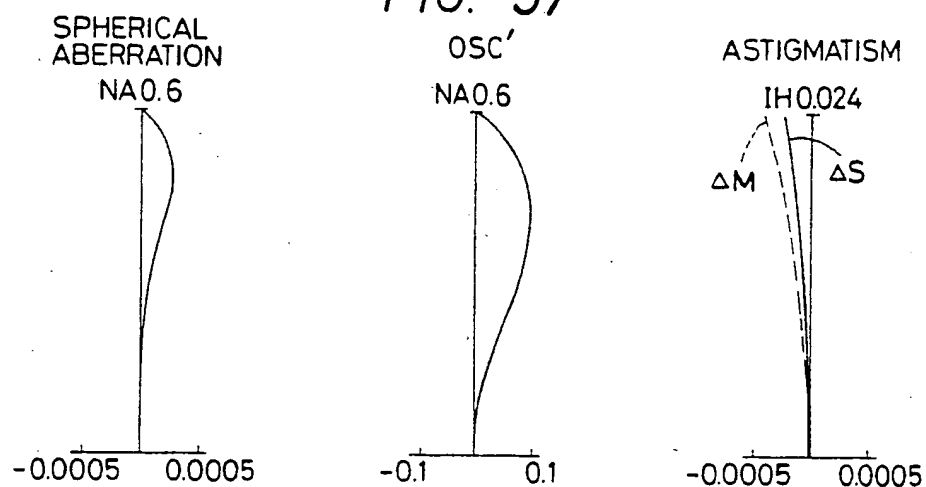


FIG. 58

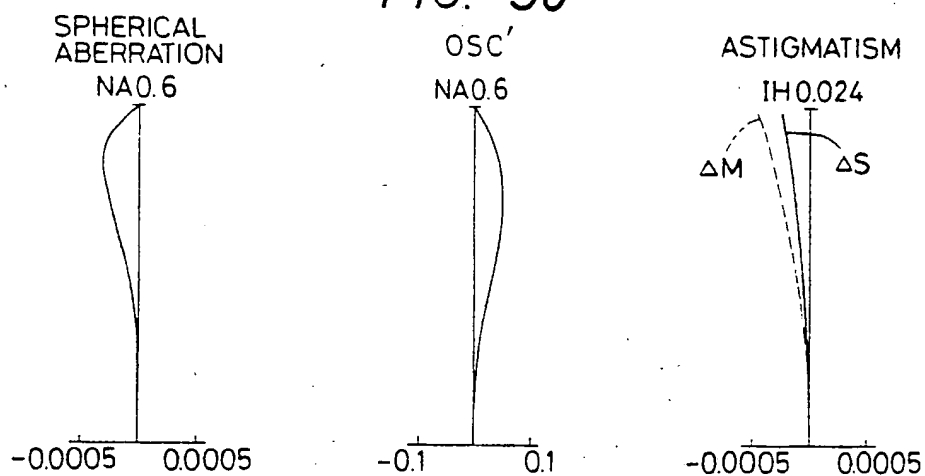


FIG. 59

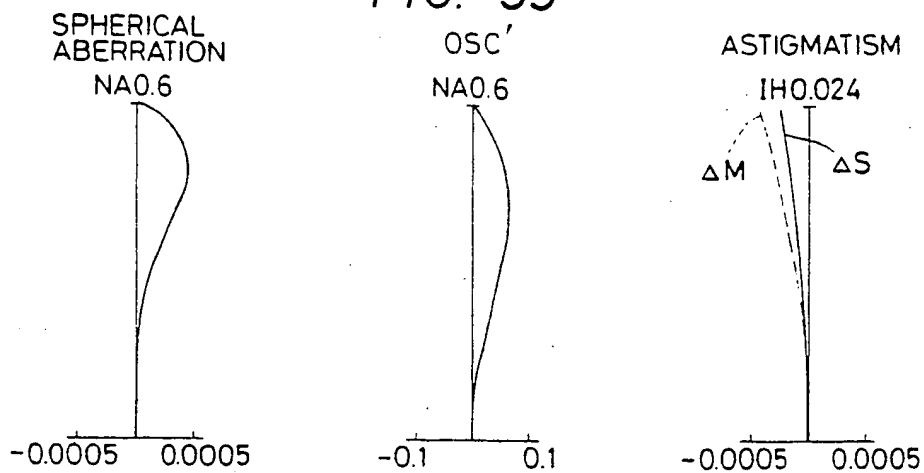


FIG. 60

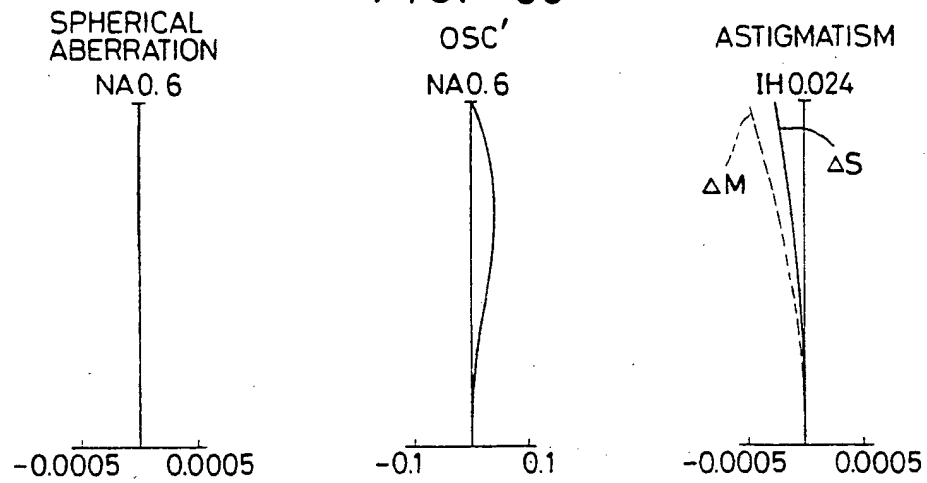


FIG. 61

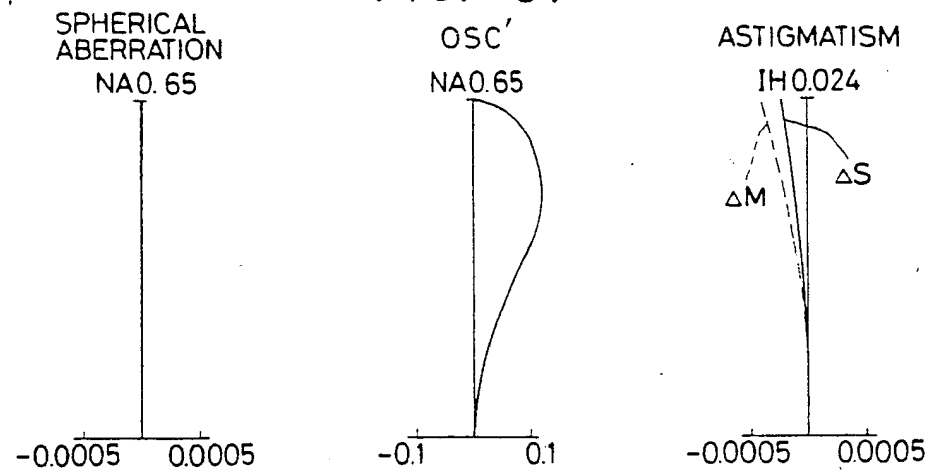


FIG. 62

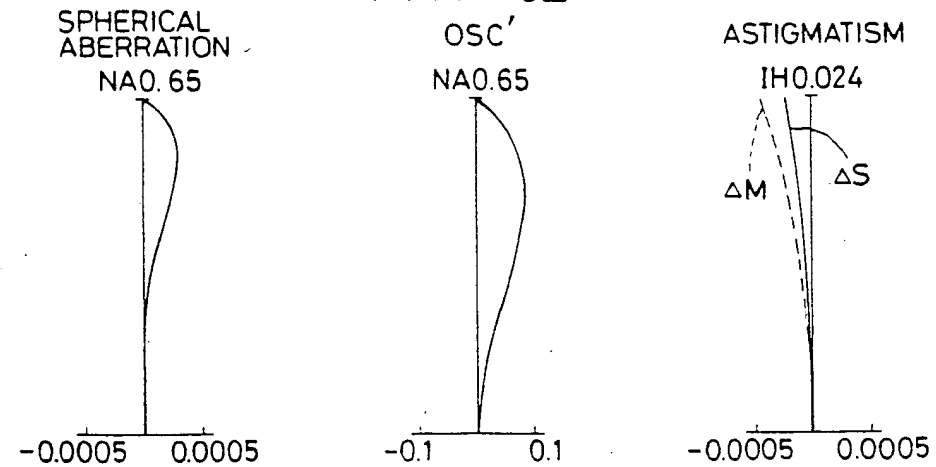


FIG. 63

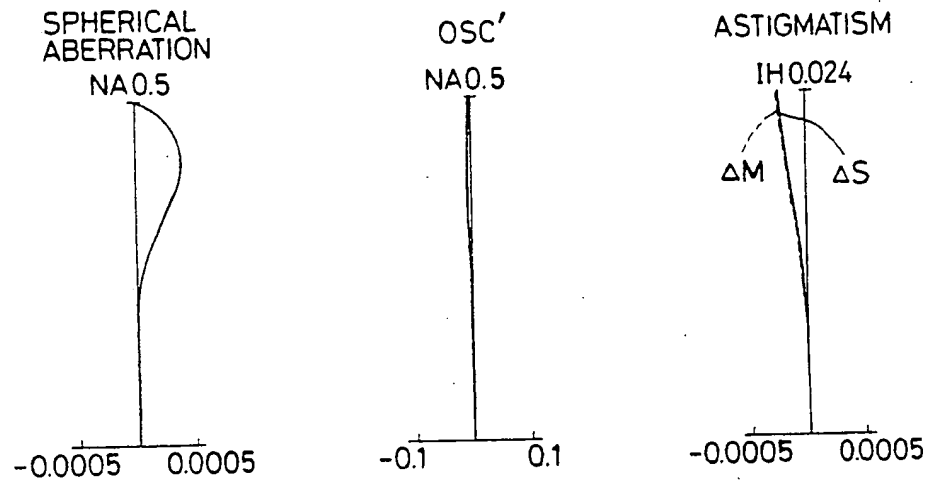


FIG. 64

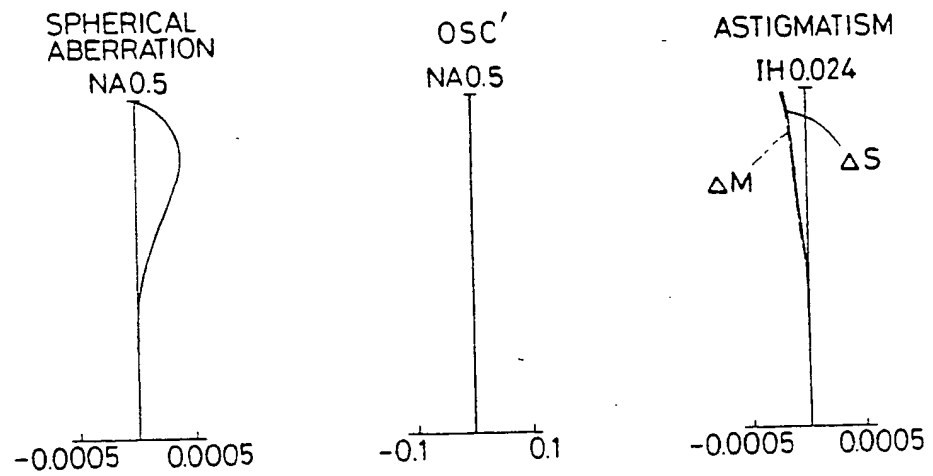


FIG. 65

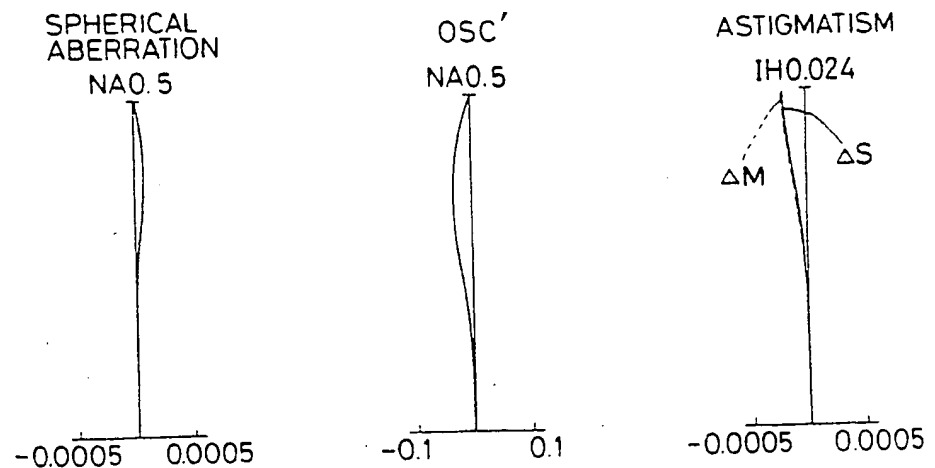


FIG. 66

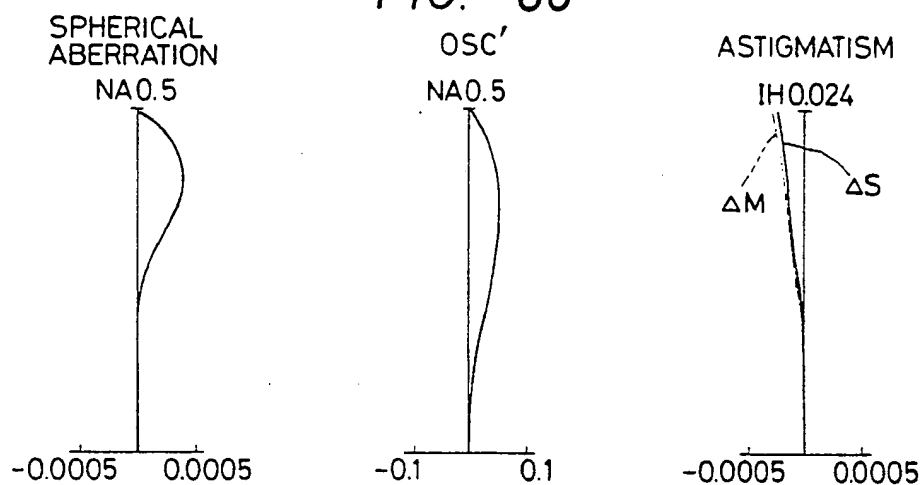


FIG. 67

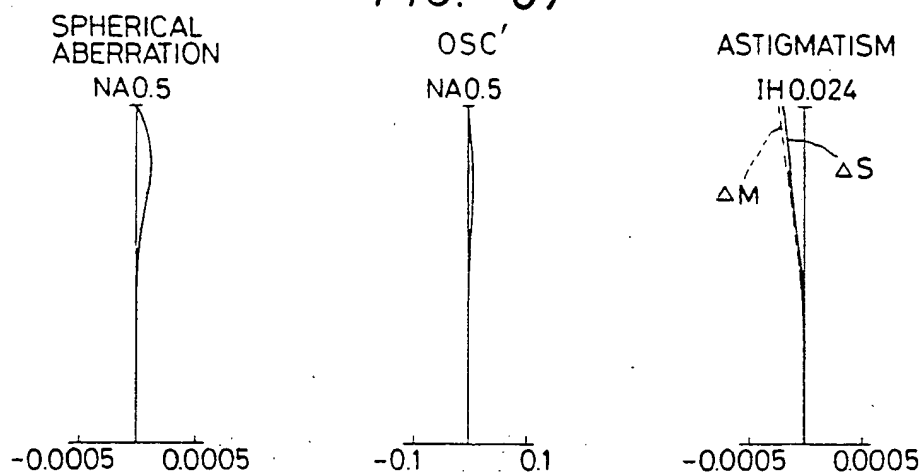


FIG. 68

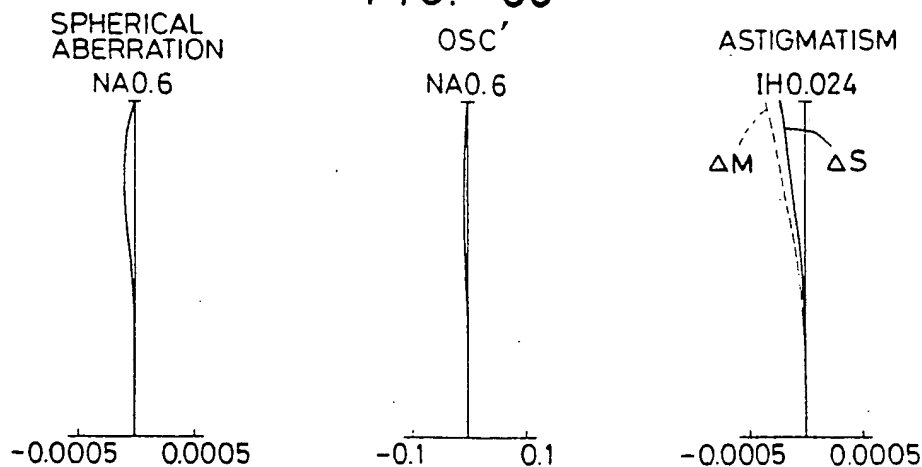


FIG. 69

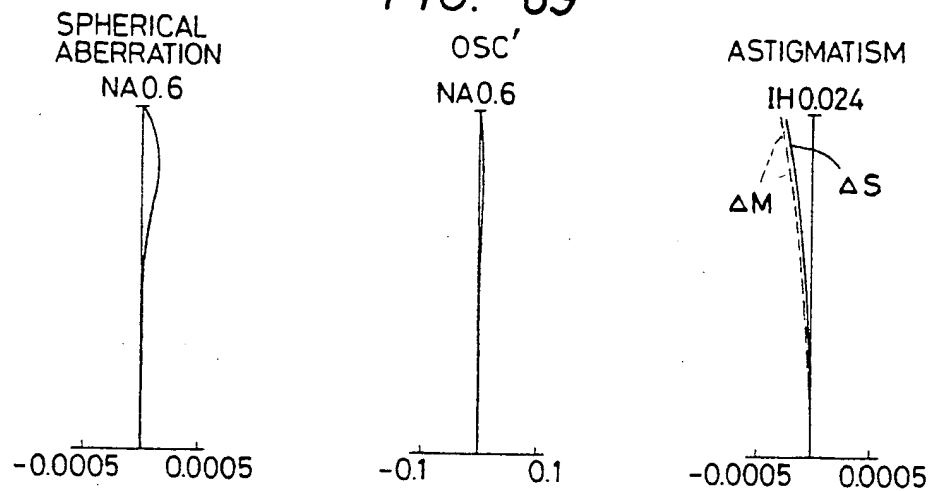


FIG. 70

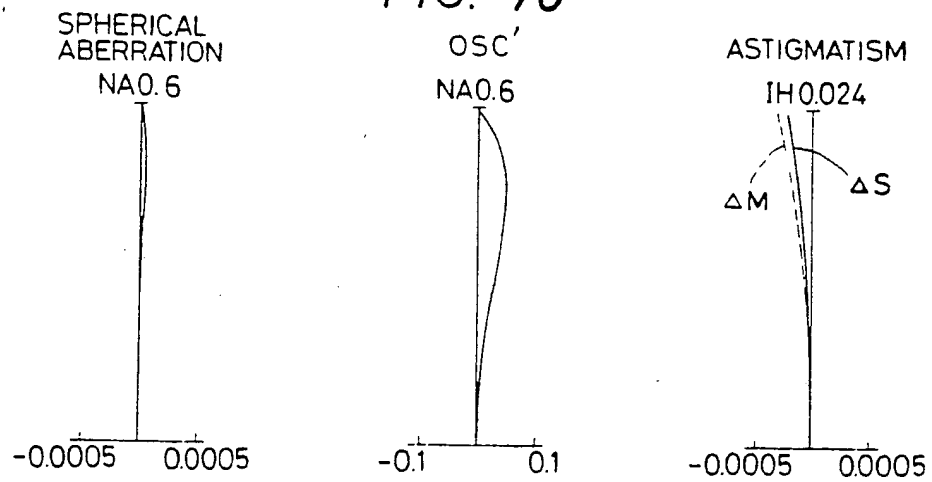


FIG. 71

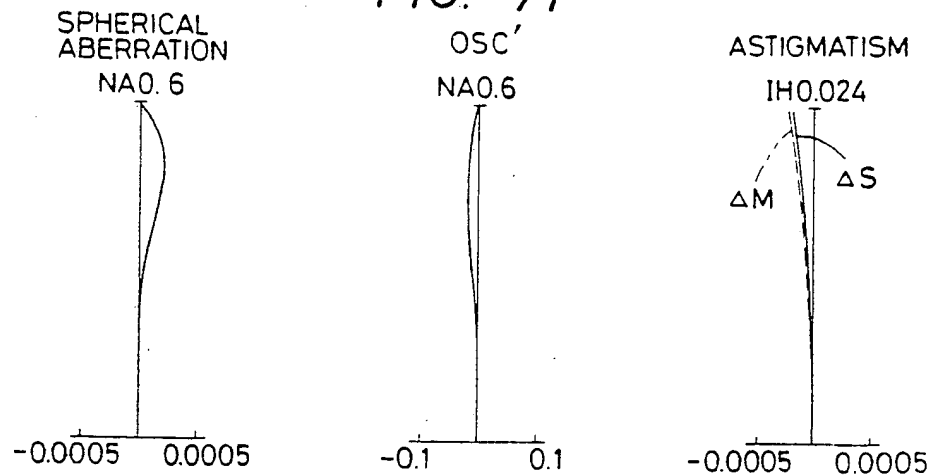


FIG. 72

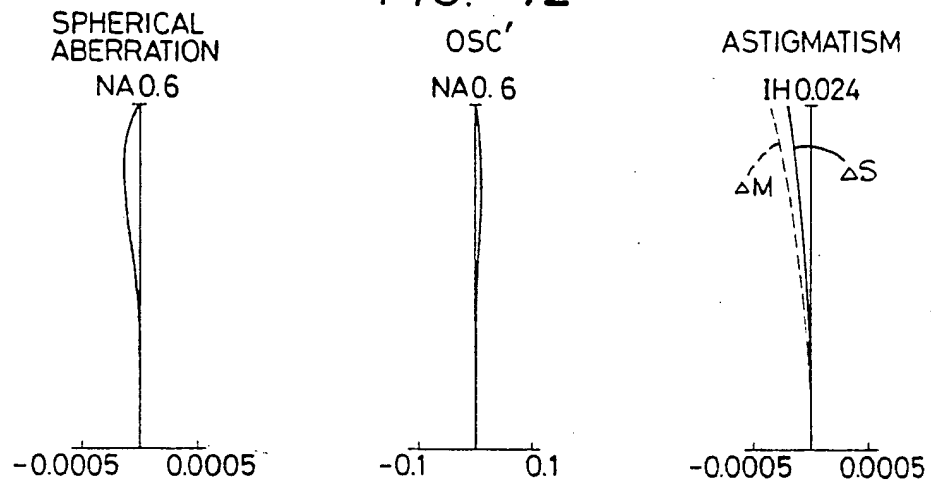


FIG. 73

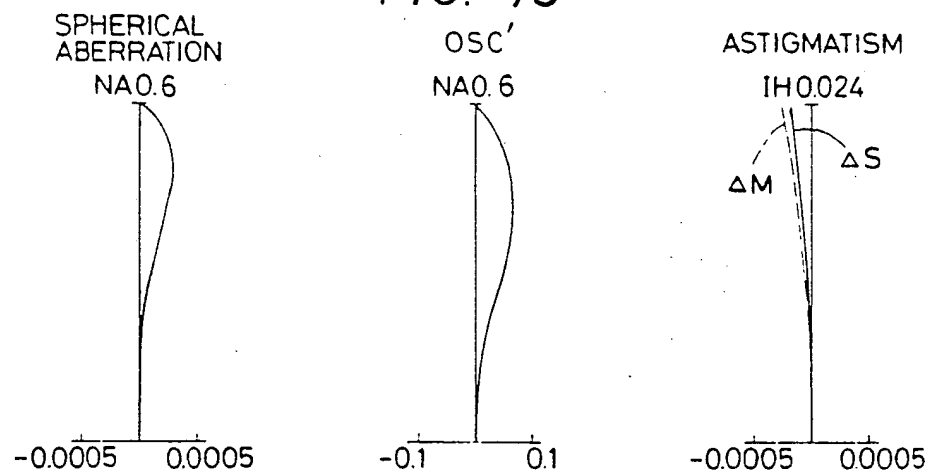


FIG. 74

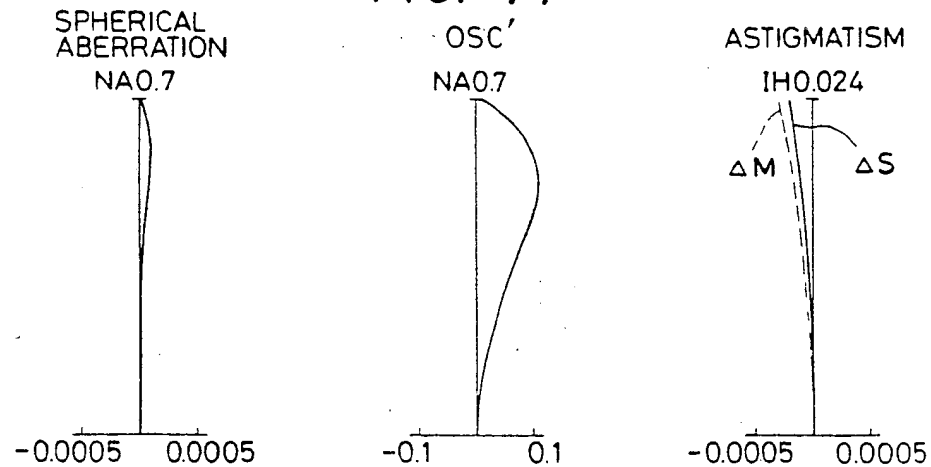
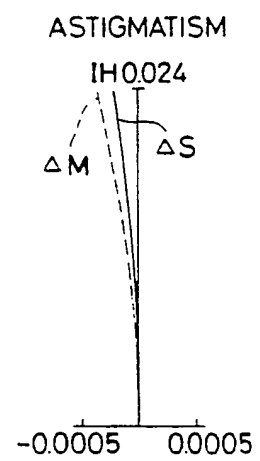
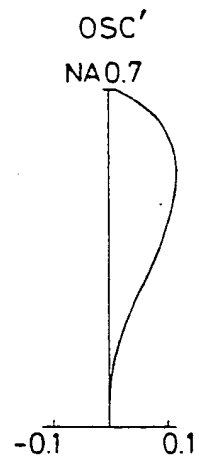
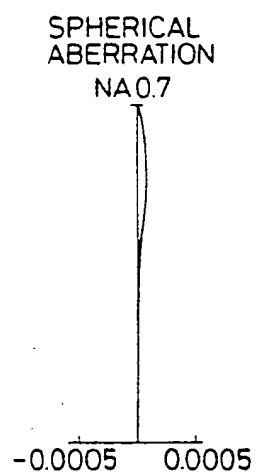


FIG. 75



SPECIFICATION

Graded refractive index lens system

- 5 a) Field of the Invention 5
The present invention relates to a lens system using inhomogeneous material, especially a graded refractive index (GRIN) single lens system used as an objective lens system for optical video disks, etc.
- 10 b) Description of the Prior Art 10
Recently there have developed apparatuses which read, by the converging of a laser beam to a microspot, the information which is recorded with high density on recording medium such as optical video disks, digital audio disks, etc.
In such apparatuses, it is necessary for an objective lens system used for the recording and the reproducing of information to be compact and light because the objective lens system is driven directly for the purpose of auto-focusing and auto-tracking. It is also necessary for the objective lens system to have a large N.A. in order to obtain a smaller spot size of a laser beam which is converged on a recording medium. 15
- As such an objective lens system, a combination of a plurality of homogeneous spherical lenses or a single homogeneous aspherical lens, especially for the purposes of being compact and light, has hitherto been in use. 20
- Moreover, besides these homogeneous lenses, a GRIN single lens system using inhomogeneous material for economy of manufacture, compactness, and light weight has been known recently. 25
- In the early GRIN lens system, only the correction of spherical aberration was considered. As is well known, it is necessary for an objective lens system used for optical video disks, etc. to have aberrations well-corrected in the range of diameters 0.1–0.2 mm on the disk surface and, therefore, not only spherical aberration but also coma should be well-corrected. 30
- A GRIN single lens system disclosed, for example, in Japanese Published Unexamined Patent Application No. 6354/80 has at least one of the refracting surfaces thereof formed as a spherical surface. In this lens system, spherical aberration is well-corrected, but the correction of other aberrations is not sufficient. 35
- GRIN single lens systems intended to correct off-axial aberrations, especially coma are disclosed in Japanese Published Unexamined Patent Application Nos. 122512/83 and 62815/84. In these lens systems, the refracting surfaces of the GRIN lens is formed as spherical one, and the radius of curvature of this spherical surface and the higher-order coefficients of the refractive index distribution are arranged so that both spherical aberration and coma can be corrected. However, in the former lens system (Japanese Published Unexamined Patent Application No. 6354/80), it cannot be said that the correction of aberrations thereof is sufficient. The latter 40
- lens systems (Japanese Published Unexamined Patent Application Nos. 122512/83 and 62815/84) have defects in that, for example, the shapes of these lenses have such strongly meniscus shapes that the manufacture thereof is difficult. 45
- Summary of the Invention*
- 45 It is a primary object of the present invention to provide a graded refractive index (GRIN) single lens system with a comparatively large N.A. comprising at least one surface thereof formed spherically, the radius of curvature of which is large so that the manufacture thereof is easy. 50
- In the GRIN single lens system according to the present invention, the refractive index distribution is cylindrically symmetric to the optical axis and is expressed by the following formula: 50
- $$n^2 = n_0^2 [1 \times (gr)^2 + h_4 (gr)^4 + h_6 (gr)^6 + \dots]$$
- where n_0 represents the refractive index on the optical axis of the lens, r represents the radial distance from the optical axis, g is the parameter representing the degree of gradient of the refractive index distribution, and, h_4 and h_6 respectively represent the 4th- and 6th-order coefficients of the refractive index distribution. 55
- In the GRIN lens whose refractive index distribution is expressed by the above mentioned formula, in order to make the refracting power of the entire lens system at a predetermined value and to correct aberrations, both the refracting power of the refracting surface and that of the lens medium are appropriately arranged. The refracting power of the lens medium can be determined precisely from the description in Journal of Optical Society of America Vol. 61, No. 7, pp.879–885, "Inhomogeneous Lens III, Paraxial Optics". According to this description, when gD is less than $\pi/2$ (D represents the thickness of the lens), the magnitude of the refractive power of the lens medium can be known by the value of gD . The degree of the gradient of the 65

refractive index distribution is expressed by the parameter g . The value of g is also influenced by the shape of the lens, for example, the diameter thereof. In an ordinary homogeneous lens, the lens whose focal length, radii of curvatures, length and diameter are multiplied by a fixed number compared with those of an original lens is optically equivalent to the original lens. In a GRIN lens, only when the parameter g is multiplied by the reciprocal of that fixed number compared with that of an original lens in addition to the values obtained as above, can the lens optically equivalent to the original lens be obtained. Therefore, the gradient of the refractive index distribution can be arranged not only by the shape of the lens but also by the value of $g\phi$ (where ϕ represents the diameter of the lens) or gf (where f represents the focal length of the lens).

Thus, in a GRIN lens, when the value of some parameters of D , gD , $g\phi$, gf , etc. are suitably chosen, and when some parameters of them are substantially selected, these selected parameters are correlated with one another and suitable values are fixed, it is possible to obtain the GRIN lens wherein N.A. is large and aberrations are well-corrected though the radius of curvature of the lens surface is kept large.

The sets of parameters to be selected may be as follows:

- (a) parameters D , gD , $g\phi$
- (b) parameters D , gf
- (c) parameters D , gD , gf
- (d) parameters D , $(g-0.5)D$

When the set (a) is selected from the above mentioned sets, it is desirable for the parameters of this set to satisfy the following conditions (1), (2), and (3):

- (1) $gD < 0.51$
- (2) $0.3 < g\phi < 0.7$
- (3) $0.28f < D$

The conditions (1) and (2) define the refracting power of the lens medium and the degree of the gradient of the refractive index distribution, and are established in order to make the radius of curvature of a refracting surface large when the aberrations are to be well-corrected.

If the value of gD becomes large, spherical aberration and coma generated by the ray passing through the lens medium will become large. In order to correct these aberrations, it is necessary to make the refracting surface at the opposite side of the long conjugate point a strong concave surface. If the value of gD under the condition (1) exceeds the limit of this condition, the radius of curvature of this surface will become strong so that the manufacture of the lens will become difficult.

Even if gD is within the limit of the condition (1), in case $g\phi$ exceeds the upper limit of the condition (2), the gradient of the refractive index distribution will become steep and the ray will be curved largely in the lens medium. In this state, it is necessary for the good correction of aberrations to make the refracting surface at the opposite side of the long conjugate point a strong concave surface, which is against the object of the present invention.

The lower limit of the condition (2) and the condition (3) itself are established in order to correct the various aberrations well. If the value of $g\phi$ under the condition (2) exceeds the lower limit of this condition or the condition (3) is not satisfied, it will be impossible to correct both spherical aberration and coma.

When the set (b) of the parameters is selected, it is necessary to satisfy the following conditions (4) and (5):

- (4) $0.96 f < D < 1.536 f$
- (5) $0.63 < gf$

The lower limit of the condition (4) and the condition (5) itself are established in order to correct both astigmatism and sign condition with good balance and, furthermore, keep the sign condition in a good state.

If the value of D under the condition (4) exceeds the lower limit thereof, astigmatism will deteriorate. If the condition (5) is not satisfied, the sign condition will deteriorate.

When these conditions are satisfied, it will be possible to correct the sign condition easily while astigmatism is kept in a good state.

The upper limit of the condition (4) is established in order to keep the minimum necessary working distance provided that the condition (5) is satisfied. In other words, if the value of D under the condition (4) exceeds the upper limit thereof, it will be impossible to keep the necessary working distance.

When the set (c) of the parameters is selected, it is necessary to satisfy the following conditions (6), (7) and (8):

- (6) $D < 1.08 f$
- (7) $gf < 0.604$
- (8) $0.51 < gD$

The condition (6) defines the length D of the lens and is established in order to keep the necessary working distance while maintaining balance with astigmatism. If this condition is not

satisfied, it will be impossible to keep a sufficient working distance.

The condition (7) is established in order to correct astigmatism. When this condition is not satisfied even if the value of D is chosen to satisfy the condition (6), astigmatism will deteriorate and it will be impossible to make N.A. large.

- 5 The upper limit of the refracting power of the lens medium is determined to satisfy the conditions (6) and (7). But in order to correct various aberrations with good balance, it is more desirable to have the refracting power distributed suitably between the power of the refracting surface and that of the lens medium. If the refracting power of the lens medium exceeds a limit value and becomes small, astigmatism will deteriorate remarkably and it will be very hard to correct it under the condition wherein astigmatism is balanced with spherical aberration. 10

The condition (8) defines the lower limit of the refracting power of the lens medium. If the value of gD under the condition (8) exceeds the lower limit thereof, it will be impossible to make N.A. large.

- 15 In the GRIN lens satisfying the conditions (6), (7) and (8), it will be possible to correct spherical aberration and astigmatism with good balance when the radius R_1 of curvature of the refracting surface at the long conjugate side and the radius R_2 of that at the short conjugate side satisfy the following condition (9) so that the refracting powers of both surfaces are well balanced: 15

$$(9) 2 < |R_2/R_1|$$

- 20 When the 4th-order coefficient h_4 of the refractive index distribution satisfy the following condition (10), it will be possible to keep a spherical aberration curve in a good shape and maintain the root mean square of wave aberration at a very small value of $\lambda/40$ near the optical axis. 20

$$(10) h_4 < 0$$

- 25 When the set (c) of the parameters, i.e., D , gf , gD is selected, even if the length D of the lens is longer to some extent, it will be possible to form the GRIN lens which also attains the object of the present invention provided that the value of gf is appropriately arranged. In other words, the following condition (11), (12) and (13) should be satisfied. 25

$$(11) 1.152 f < D < 1.392 f$$

- 30 (12) $gf < 0.562$ 30

$$(13) 0.51 < gD$$

The lower limit of the condition (11) and the upper limit of the condition (12) are established in order to correct astigmatism. If these limits are exceeded, it will be impossible to correct astigmatism sufficiently when N.A. is to be large.

- 35 The upper limit of the condition (11) is established in order to make the radius of curvature of at least one refracting surface large. If the value of D under the condition (11) exceeds the upper limit thereof, it will be impossible to make the radius of the refracting surface large. 35

The condition (13) is established for the same reason as for the establishment of the condition (8).

- 40 Finally, when the set (d) of the parameters is selected, it will be necessary to satisfy the following conditions (14) and (15). 40

$$(14) 1.54 f < D$$

$$(15) -4 < (g - 0.5)D$$

- 45 The condition (14) relates to the length of the lens and is to correct astigmatism. If this condition is not satisfied, it will be impossible to correct astigmatism when N.A. is enlarged to about 0.7. 45 ✓✓

- The condition (15) relates to the refracting power of the lens medium. As is mentioned above, in a GRIN lens, the refracting power of the entire lens can be divided between the refracting power of the refracting surface and that of the lens medium, the balance of which is important when the various aberrations are to be corrected. For keeping a good balance it is necessary to take the length of the lens itself into account. If this condition (15) is not satisfied, spherical aberration will deteriorate. Depending on the refracting power of the refracting surface, it may be hard to keep a good balance of aberrations and impossible to correct them. 50

- 55 *Brief Description of the Drawings* 55

Figure 1 shows a sectional view of Embodiment 1 of the GRIN single lens system according to the present invention;

Figure 2 shows a sectional view of Embodiments 2, 3, 4, 20 and 21 of the GRIN single lens system according to the present invention;

- 60 Figure 3 shows a sectional view of Embodiments 5 through 19 of the GRIN single lens system according to the present invention; 60

Figure 4 shows a sectional view of Embodiments 22, 23, 24, 25, 27 and 31 of the GRIN single lens system according to the present invention;

- 65 Figure 5 shows a sectional view of Embodiments 26, 28, 29, 30 and 32 of the GRIN single lens system according to the present invention; 65

Figure 6 shows a sectional view of Embodiments 33, 34, 40 and 41 of the GRIN single lens system according to the present invention;

Figure 7 shows a sectional view of Embodiments 35, 36, 37, 38, 39 and 41 of the GRIN single lens system according to the present invention;

5 Figure 8 shows a sectional view of Embodiment 44 of the GRIN single lens system according to the present invention; 5

Figure 9 shows a sectional view of Embodiments 43, 45, 46, 47, 48, 49, 50 and 51 of the GRIN single lens system according to the present invention;

10 Figure 10 shows a sectional view of Embodiments 52, 53, 54, 55, 56, 58, 59, 60 and 62 of the GRIN single lens system according to the present invention; 10

Figure 11 shows a sectional view of Embodiments 57, 61, 63 and 64 of the GRIN single lens system according to the present invention; and

15 Figure 12 through 75, respectively, shows graphs illustrating aberration curves of Embodiment 1 through 64 of the GRIN lens system according to the present invention. 15

Detailed Description of the Preferred Embodiments

Preferred Embodiments of the GRIN lens system according to the present invention as described above are explained below.

20 Embodiments 1 through 21 according to the present invention shown in the following numerical data have the features in the parameters gD , $g\phi$, D defined and satisfy the conditions (1), (2) and (3). 20

Embodiment 1

25 $R_1 = 2.847$ $R_2 = \infty$ $D = 2.832$ $n_0 = 1.65$ 25
 $g = 0.12$ $h_4 = 2.404$ $h_6 = 47.99$ $\phi = 3.2$
 30 $f = 3.5556$ $NA = 0.45$ $WD = 1.21$ $gD = 0.340$ 30
 $g\phi = 0.384$ $D/f = 0.796$

35 35

Embodiment 2

40 $R_1 = 3.009$ $R_2 = -62.404$ $D = 3.333$ $n_0 = 1.65$ 40
 $g = 0.12$ $h_4 = 1.716$ $h_6 = 32.20$ $\phi = 3.2$
 $f = 3.5556$ $NA = 0.45$ $WD = 0.99$ $gD = 0.400$
 45 $g\phi = 0.384$ $D/f = 0.937$ 45

50 Embodiment 3 50

$R_1 = 3.194$ $R_2 = -24.832$ $D = 3.750$ $n_0 = 1.65$
 55 $g = 0.12$ $h_4 = 1.298$ $h_6 = 23.65$ $\phi = 3.2$ 55
 $f = 3.5556$ $NA = 0.45$ $WD = 0.84$ $gD = 0.45$
 $g\phi = 0.384$ $D/f = 1.055$

Embodiment 4

	$R_1 = 3.458$	$R_2 = -12.852$	$D = 4.167$	$n_0 = 1.65$	
5	$g = 0.12$	$h_4 = 1.082$	$h_6 = 18.89$	$\phi = 3.2$	5
	$f = 3.5556$	$NA = 0.45$	$WD = 0.73$	$gD = 0.5$	
10	$g\phi = 0.384$	$D/f = 1.172$			10

Embodiment 5

15	$R_1 = 2.649$	$R_2 = 60.550$	$D = 1.333$	$n_0 = 1.65$	15
	$g = 0.15$	$h_4 = -0.597$	$h_6 = -2.040$	$\phi = 3.2$	
20	$f = 3.5556$	$NA = 0.45$	$WD = 2.01$	$gD = 0.2$	20
	$g\phi = 0.48$	$D/f = 0.375$			
25					25

Embodiment 6

30	$R_1 = 2.716$	$R_2 = 40.040$	$D = 1.667$	$n_0 = 1.65$	30
	$g = 0.15$	$h_4 = -0.611$	$h_6 = -0.923$	$\phi = 3.2$	
	$f = 3.5556$	$NA = 0.45$	$WD = 1.82$	$gD = 0.25$	
35	$g\phi = 0.48$	$D/f = 0.469$			35

Embodiment 7

40	$R_1 = 2.792$	$R_2 = 30.725$	$D = 2.0$	$n_0 = 1.65$	40
	$g = 0.15$	$h_4 = -0.646$	$h_6 = -0.816$	$\phi = 3.2$	
45	$f = 3.5556$	$NA = 0.45$	$WD = 1.64$	$gD = 0.3$	45
	$g\phi = 0.48$	$D/f = 0.562$			
50					50

Embodiment 8

55	$R_1 = 2.877$	$R_2 = 25.630$	$D = 2.333$	$n_0 = 1.65$	55
	$g = 0.15$	$h_4 = -0.691$	$h_6 = -0.993$	$\phi = 3.2$	
60	$f = 3.5556$	$NA = 0.45$	$WD = 1.45$	$gD = 0.35$	60
	$g\phi = 0.48$	$D/f = 0.656$			

Embodiment 9

	$R_1 = 2.973$	$R_2 = 22.668$	$D = 2.667$	$n_0 = 1.65$	
5	$g = 0.15$	$h_4 = -0.735$	$h_6 = -1.227$	$\phi = 3.2$	5
	$f = 3.5556$	$NA = 0.45$	$WD = 1.28$	$gD = 0.4$	
10	$g\phi = 0.48$	$D/f = 0.750$			10

Embodiment 10

15	$R_1 = 3.081$	$R_2 = 21.061$	$D = 3.0$	$n_0 = 1.65$	15
	$g = 0.15$	$h_4 = -0.774$	$h_6 = -1.420$	$\phi = 3.2$	
20	$f = 3.5556$	$NA = 0.45$	$WD = 1.11$	$gD = 0.45$	20
	$g\phi = 0.48$	$D/f = 0.844$			
25					25

Embodiment 11

30	$R_1 = 3.206$	$R_2 = 20.562$	$D = 3.333$	$n_0 = 1.65$	30
	$g = 0.15$	$h_4 = -0.802$	$h_6 = -1.526$	$\phi = 3.2$	
35	$f = 3.5556$	$NA = 0.45$	$WD = 0.95$	$gD = 0.5$	35
	$g\phi = 0.48$	$D/f = 0.937$			
40					40

Embodiment 12

45	$R_1 = 2.916$	$R_2 = 17.811$	$D = 2.059$	$n_0 = 1.65$	45
	$g = 0.17$	$h_4 = -1.247$	$h_6 = -5.704$	$\phi = 3.2$	
50	$f = 3.5556$	$NA = 0.45$	$WD = 1.59$	$gD = 0.35$	50
	$g\phi = 0.544$	$D/f = 0.579$			

Embodiment 13

55	$R_1 = 3.009$	$R_2 = 14.981$	$D = 2.353$	$n_0 = 1.65$	55
	$g = 0.17$	$h_4 = -1.163$	$h_6 = -4.370$	$\phi = 3.2$	
60	$f = 3.5556$	$NA = 0.45$	$WD = 1.44$	$gD = 0.4$	60
	$g\phi = 0.544$	$D/f = 0.662$			
65					65

Embodiment 14

	$R_1 = 3.110$	$R_2 = 12.932$	$D = 2.647$	$n_0 = 1.65$	
5	$g = 0.17$	$h_4 = -1.099$	$h_6 = -3.524$	$\phi = 3.2$	5
	$f = 3.5556$	$NA = 0.45$	$WD = 1.28$	$gD = 0.45$	
10	$g\phi = 0.544$	$D/f = 0.744$			10

Embodiment 15

15	$R_1 = 3.219$	$R_2 = 11.371$	$D = 2.941$	$n_0 = 1.65$	15
	$g = 0.17$	$h_4 = -1.047$	$h_6 = -2.937$	$\phi = 3.2$	
20	$f = 3.5556$	$NA = 0.45$	$WD = 1.12$	$gD = 0.5$	20
	$g\phi = 0.544$	$D/f = 0.827$			
25					25

Embodiment 16

30	$R_1 = 3.206$	$R_2 = 9.178$	$D = 2.250$	$n_0 = 1.65$	30
	$g = 0.20$	$h_4 = -1.092$	$h_6 = -2.748$	$\phi = 3.2$	
	$f = 3.5556$	$NA = 0.45$	$WD = 1.48$	$gD = 0.45$	
35	$g\phi = 0.64$	$D/f = 0.633$			35

Embodiment 17

40	$R_1 = 3.318$	$R_2 = 7.883$	$D = 2.5$	$n_0 = 1.65$	40
	$g = 0.20$	$h_4 = -0.986$	$h_6 = -2.099$	$\phi = 3.2$	
	$f = 3.5556$	$NA = 0.45$	$WD = 1.34$	$gD = 0.5$	
50	$g\phi = 0.64$	$D/f = 0.703$			50

Embodiment 18

55	$R_1 = 3.148$	$R_2 = 65.733$	$D = 3.5$	$n_0 = 1.7$	55
	$g = 0.12$	$h_4 = 0.909$	$h_6 = 19.14$	$\phi = 3.2$	
60	$f = 3.5556$	$NA = 0.45$	$WD = 0.89$	$gD = 0.42$	60
	$g\phi = 0.384$	$D/f = 0.984$			

Embodiment 19

	$R_1 = 3.149$	$R_2 = 10.286$	$D = 2.5$	$n_0 = 1.7$	
5	$g = 0.17$	$h_4 = -1.169$	$h_6 = -3.832$	$\phi = 3.2$	5
	$f = 3.5556$	$NA = 0.45$	$WD = 1.34$	$gD = 0.425$	
10	$g\phi = 0.544$	$D/f = 0.703$			10

Embodiment 20

15	$R_1 = 2.760$	$R_2 = -14.835$	$D = 3.0$	$n_0 = 1.55$	15
	$g = 0.13$	$h_4 = 1.839$	$h_6 = 36.50$	$\phi = 3.2$	
20	$f = 3.5556$	$NA = 0.45$	$WD = 1.18$	$gD = 0.39$	20
	$g\phi = 0.416$	$D/f = 0.844$			

Embodiment 21

30	$R_1 = 2.512$	$R_2 = -43.624$	$D = 1.5$	$n_0 = 1.55$	30
	$g = 0.16$	$h_4 = -0.608$	$h_6 = -2.217$	$\phi = 3.2$	
	$f = 3.5556$	$NA = 0.45$	$WD = 1.93$	$gD = 0.24$	
35	$g\phi = 0.512$	$D/f = 0.422$			35

where R_1 , R_2 respectively represent the radii of curvatures of the lens surfaces, D represents the length of the lens, n_0 represents the refractive index on the optical axis of the lens, the parameter g represents the gradient of the refractive index distribution, h_4 and h_6 respectively represent the 4th- and 6th-order coefficients of the refractive index distribution, ϕ represents the diameter of the lens, f represents the focal length of the lens, NA represents the numerical aperture at the side of the disk, and WD represents the distance between the lens and the disk. Both the coefficient g of the refractive index distribution and the value of refractive index are for the wave length $\lambda = 780$ nm.

Embodiments 1 through 21 according to the present invention respectively satisfy the conditions (1) through (3).

Embodiment 1 according to the present invention is shown in Fig. 1 and is a plano-convex lens having a convex surface at a light source side not shown in this figure (at a long conjugate side). Each of Embodiments 2, 3, 4, 20 and 21 according to the present invention is, as shown in Fig. 2, a biconvex lens having a stronger convex surface at a light source side. Each of Embodiments 5 through 19 is, as shown in Fig. 3, a positive meniscus lens having convex surface at a light source side.

Embodiments 22 through 32 according to the present invention shown in the following numerical data are the lenses satisfying the conditions (4) and (5).

Embodiment 22

60	$R_1 = 1.234$	$R_2 = 7.004$	$D = 1.440$	$n_0 = 1.50$	60
	$g = 0.646$	$h_4 = -0.500$	$h_6 = -0.426$	$f = 1.0$	
	$NA = 0.5$				

Embodiment 23

	$R_1 = 1.013$	$R_2 = 4.115$	$D = 1.140$	$n_0 = 1.50$	
5	$g = 0.667$	$h_4 = -0.718$	$h_6 = -1.144$	$f = 1.0$	5
	$NA = 0.5$				

10

10

Embodiment 24

	$R_1 = 1.167$	$R_2 = 1.230$	$D = 1.320$	$n_0 = 1.50$	
15	$g = 0.708$	$h_4 = -0.530$	$h_6 = -0.501$	$f = 1.0$	15
	$NA = 0.5$				

20

20

Embodiment 25

	$R_1 = 1.039$	$R_2 = 1.719$	$D = 1.080$	$n_0 = 1.50$	
25	$g = 0.729$	$h_4 = -0.640$	$h_6 = -0.809$	$f = 1.0$	25
	$NA = 0.5$				
30					30

Embodiment 26

	$R_1 = 1.190$	$R_2 = 0.699$	$D = 1.200$	$n_0 = 1.50$	
35	$g = 0.792$	$h_4 = -0.385$	$h_6 = -0.221$	$f = 1.0$	35
	$NA = 0.5$				
40					40

45 Embodiment 27

45

	$R_1 = 1.025$	$R_2 = 1.462$	$D = 1.080$	$n_0 = 1.65$	
	$g = 0.646$	$h_4 = -0.847$	$h_6 = -1.547$	$f = 1.0$	
50	$NA = 0.5$				50

55 Embodiment 28

55

	$R_1 = 1.244$	$R_2 = 0.630$	$D = 1.368$	$n_0 = 1.65$	
60	$g = 0.688$	$h_4 = -0.533$	$h_6 = -0.501$	$f = 1.0$	60
	$NA = 0.5$				

Embodiment 29

$R_1 = 1.117$ $R_2 = 0.874$ $D = 1.140$ $n_0 = 1.65$
 5 $g = 0.708$ $h_4 = -0.628$ $h_6 = -0.719$ $f = 1.0$ 5
 $NA = 0.5$

10

Embodiment 30

$R_1 = 1.103$ $R_2 = 0.902$ $D = 1.020$ $n_0 = 1.65$
 15 $g = 0.750$ $h_4 = -0.570$ $h_6 = -0.568$ $f = 1.0$ 15
 $NA = 0.5$

20

Embodiment 31

$R_1 = 1.231$ $R_2 = 2.313$ $D = 1.440$ $n_0 = 1.50$
 25 $g = 0.667$ $h_4 = -0.510$ $h_6 = -0.489$ $f = 1.0$ 25
 $NA = 0.6$

30

Embodiment 32

$R_1 = 1.213$ $R_2 = 1.065$ $D = 1.380$ $n_0 = 1.50$
 35 $g = 0.708$ $h_4 = -0.488$ $h_6 = -0.432$ $f = 1.0$ 35
 $NA = 0.6$

40

where R_1 , R_2 respectively represent the radii of curvatures of the lens surfaces, D represents the length of the lens, n_0 represents the refractive index on the optical axis of the lens, the parameter g represents the gradient of the refractive index distribution, h_4 and h_6 respectively represent the 4th- and 6th-order coefficients of the refractive index distribution, f represents the focal length of the lens, and NA represents the numerical aperture at the side of the disk. Both the coefficient g of the refractive index distribution and the value of refractive index are for the wave length $\lambda = 780$ nm.

Among them, each of Embodiments 22 through 25, 27 and 31 according to the present invention is a positive meniscus lens as shown in Fig. 4. Each of Embodiments 26, 28 through 30 and 32 according to the present invention is a negative meniscus lens as shown in Fig. 5.

Embodiments 33 through 42 according to the present invention shown in the following numerical data are the lenses satisfying the conditions (6) through (8), and also satisfying the conditions (9) and (10).

55

Embodiment 33

$R_1 = 0.866$ $R_2 = -4.095$ $D = 1.02$ $n_0 = 1.5$
 60 $g = 0.563$ $h_4 = -0.468$ $h_6 = 0.822$ $f = 1.0$ 60
 $NA = 0.5$ $WD = 0.283$

Embodiment 34

	$R_1 = 0.815$	$R_2 = -9.840$	$D = 0.876$	$n_0 = 1.5$	
5	$g = 0.592$	$h_4 = -0.704$	$h_6 = -1.402$	$f = 1.0$	5
	$NA = 0.5$	$WD = 0.340$			

10

10

Embodiment 35

15	$R_1 = 0.903$	$R_2 = 5.311$	$D = 1.010$	$n_0 = 1.65$	15
	$g = 0.521$	$h_4 = -0.699$	$h_6 = -0.666$	$f = 1.0$	
	$NA = 0.5$	$WD = 0.259$			

20

20

Embodiment 36

25	$R_1 = 0.966$	$R_2 = 2.452$	$D = 1.060$	$n_0 = 1.65$	25
	$g = 0.585$	$h_4 = -0.936$	$h_6 = -2.223$	$f = 1.0$	
30	$NA = 0.5$	$WD = 0.223$			30

Embodiment 37

35	$R_1 = 0.905$	$R_2 = 20.534$	$D = 1.070$	$n_0 = 1.65$	35
	$g = 0.479$	$h_4 = -0.210$	$h_6 = 4.469$	$f = 1.0$	
40	$NA = 0.5$	$WD = 0.240$			40

45 Embodiment 38

45

	$R_1 = 0.932$	$R_2 = 3.942$	$D = 1.050$	$n_0 = 1.65$	
50	$g = 0.542$	$h_4 = -0.846$	$h_6 = -1.904$	$f = 1.0$	50
	$NA = 0.55$	$WD = 0.237$			

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Embodiment 39

	$R_1 = 0.891$	$R_2 = 3.727$	$D = 0.924$	$n_0 = 1.65$	
60	$g = 0.554$	$h_4 = -0.886$	$h_6 = -2.415$	$f = 1.0$	60
	$NA = 0.55$	$WD = 0.295$			

Embodiment 40

	$R_1 = 0.871$	$R_2 = -6.682$	$D = 1.020$	$n_0 = 1.5$	
5	$g = 0.583$	$h_4 = -0.657$	$h_6 = -0.832$	$f = 1.0$	5
	$NA = 0.6$	$WD = 0.275$			

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Embodiment 41

	$R_1 = 0.816$	$R_2 = -8.201$	$D = 0.900$	$n_0 = 1.5$	
15	$g = 0.583$	$h_4 = -0.649$	$h_6 = -0.860$	$f = 1.0$	15
	$NA = 0.6$	$WD = 0.329$			

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Embodiment 42

25	$R_1 = 0.915$	$R_2 = 7.404$	$D = 1.070$	$n_0 = 1.65$	25
	$g = 0.504$	$h_4 = -0.579$	$h_6 = 0.942$	$f = 1.0$	
30	$NA = 0.6$	$WD = 0.234$			30

wherein R_1 , R_2 respectively represent the radii of curvatures of the lens surfaces, D represents the length of the lens, n_0 represents the refractive index on the optical axis of the lens, the parameter g represents the gradient of the refractive index distribution, h_4 and h_6 respectively represent the 4th- and 6th-order coefficients of the refractive index distribution, f represents the focal length of the lens, NA represents the numerical aperture at the side of the disk, and WD represents the distance between the lens and the disk. Both the coefficient g of the refractive index distribution and the value of refractive index are for the wave length $\lambda=780$ nm.

Among them, each of Embodiments 33, 34, 40 and 41 according to the present invention is a biconvex lens as shown in Fig. 6, and each of Embodiments 35 through 39 and 42 is a positive meniscus lens as shown in Fig. 7.

Each of Embodiments 43 through 51 according to the present invention shown in the following numerical data are the lenses satisfying the conditions (11) through (13).

45 Embodiment 43

45

	$R_1 = 1.075$	$R_2 = 16.903$	$D = 1.320$	$n_0 = 1.65$	
50	$g = 0.521$	$h_4 = -0.693$	$h_6 = -0.677$	$f = 1.0$	50
	$NA = 0.5$				

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Embodiment 44

	$R_1 = 1.069$	$R_2 = -15.880$	$D = 1.368$	$n_0 = 1.80$	
60	$g = 0.375$	$h_4 = 1.058$	$h_6 = 21.635$	$f = 1.0$	60
	$NA = 0.5$				

Embodiment 45

$R_1 = 1.035$ $R_2 = 2.0750$ $D = 1.248$ $n_0 = 1.80$
 5 $g = 0.479$ $h_4 = -0.954$ $h_6 = -2.156$ $f = 1.0$
 $NA = 0.5$

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Embodiment 46

$R_1 = 1.022$ $R_2 = 115.424$ $D = 1.272$ $n_0 = 1.65$
 15 $g = 0.500$ $h_4 = -0.602$ $h_6 = 0.441$ $f = 1.0$
 $NA = 0.6$

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Embodiment 47

25 $R_1 = 1.002$ $R_2 = 4.042$ $D = 1.200$ $n_0 = 1.65$
 $g = 0.542$ $h_4 = -0.844$ $h_6 = -1.800$ $f = 1.0$
 30 $NA = 0.6$

30

Embodiment 48

35 $R_1 = 1.039$ $R_2 = 5.178$ $D = 1.320$ $n_0 = 1.80$
 $g = 0.417$ $h_4 = -0.296$ $h_6 = 5.302$ $f = 1.0$
 40 $NA = 0.6$

40

Embodiment 49

45 $R_1 = 1.059$ $R_2 = 2.671$ $D = 1.320$ $n_0 = 1.80$
 $g = 0.458$ $h_4 = -0.854$ $h_6 = -1.367$ $f = 1.0$
 50 $NA = 0.6$

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Embodiment 50

60 $R_1 = 1.060$ $R_2 = 10.703$ $D = 1.320$ $n_0 = 1.65$
 $g = 0.521$ $h_4 = -0.741$ $h_6 = -0.911$ $f = 1.0$
 $NA = 0.65$

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Embodiment 51

$$R_1 = 1.074 \quad R_2 = 3.970 \quad D = 1.368 \quad n_0 = 1.80$$

$$g = 0.438 \quad h_4 = -0.682 \quad h_6 = -0.661 \quad f = 1.0$$

$$NA = 0.65$$

where R_1 , R_2 respectively represent the radii of curvatures of the lens surfaces, D represents the length of the lens, n_0 represents the refractive index on the optical axis of the lens, the parameter g represents the gradient of the refractive index distribution, h_4 and h_6 respectively represent the 4th- and 6th-order coefficients of the refractive index distribution, f represents the focal length of the lens, and NA represents the numerical aperture at the side of the disk. Both the coefficient g of the refractive index distribution and the value of refractive index are for the wave length $\lambda = 780$ nm.

Among them, each of Embodiments 43, 45 through 51 according to the present invention is a positive meniscus lens as shown in Fig. 9, and Embodiment 44 according to the present invention is a biconvex lens as shown in Fig. 8.

* Embodiments 52 through 64 according to the present invention shown in the following the numerical data are the lenses satisfying the conditions (14) and (15).

Embodiment 52

$$R_1 = 1.697 \quad R_2 = -1.356 \quad D = 1.56 \quad n_0 = 1.5$$

$$g = 0.583 \quad h_4 = 0.208 \quad h_6 = 1.640 \quad f = 1.0$$

$$NA = 0.5$$

Embodiment 53

$$R_1 = 1.830 \quad R_2 = -1.518 \quad D = 1.68 \quad n_0 = 1.65$$

$$g = 0.500 \quad h_4 = 0.530 \quad h_6 = 3.966 \quad f = 1.0$$

$$NA = 0.5$$

Embodiment 54

$$R_1 = 2.195 \quad R_2 = -1.807 \quad D = 1.92 \quad n_0 = 1.65$$

$$g = 0.542 \quad h_4 = 0.120 \quad h_6 = 0.561 \quad f = 1.0$$

$$NA = 0.5$$

Embodiment 55

$$R_1 = 1.332 \quad R_2 = -2.166 \quad D = 1.56 \quad n_0 = 1.8$$

$$g = 0.375 \quad h_4 = 1.755 \quad h_6 = 26.713 \quad f = 1.0$$

$$NA = 0.5$$

Embodiment 56

$R_1 = 1.657$ $R_2 = -3.000$ $D = 1.80$ $n_0 = 1.8$
 5 $g = 0.458$ $h_4 = -0.103$ $h_6 = 1.743$ $f = 1.0$ 5
 $NA = 0.5$

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Embodiment 57

$R_1 = 1.355$ $R_2 = 1.906$ $D = 1.56$ $n_0 = 1.5$
 15 $g = 0.667$ $h_4 = -0.415$ $h_6 = -0.316$ $f = 1.0$ 15
 $NA = 0.6$

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Embodiment 58

$R_1 = 1.500$ $R_2 = -4.096$ $D = 1.62$ $n_0 = 1.5$
 25 $g = 0.625$ $h_4 = -0.268$ $h_6 = 0.024$ $f = 1.0$ 25
 30 $NA = 0.6$ 30

Embodiment 59

$R_1 = 1.303$ $R_2 = -374.044$ $D = 1.56$ $n_0 = 1.65$
 35 $g = 0.542$ $h_4 = -0.570$ $h_6 = -0.430$ $f = 1.0$ 35
 40 $NA = 0.6$ 40

45 Embodiment 60

45

$R_1 = 1.771$ $R_2 = -2.650$ $D = 1.80$ $n_0 = 1.65$
 50 $g = 0.542$ $h_4 = -0.130$ $h_6 = 0.446$ $f = 1.0$ 50
 $NA = 0.6$

55 Embodiment 61

55

$R_1 = 1.389$ $R_2 = 2.792$ $D = 1.68$ $n_0 = 1.8$
 60 $g = 0.500$ $h_4 = -0.747$ $h_6 = -1.277$ $f = 1.0$ 60
 $NA = 0.6$

Embodiment 62

$R_1 = 1.322$ $R_2 = -7.400$ $D = 1.62$ $n_0 = 1.8$
 5 $g = 0.438$ $h_4 = -0.410$ $h_6 = 1.969$ $f = 1.0$ 5
 $NA = 0.6$

10

Embodiment 63

$R_1 = 1.289$ $R_2 = 47.625$ $D = 1.56$ $n_0 = 1.65$
 15 $g = 0.542$ $h_4 = -0.601$ $h_6 = -0.530$ $f = 1.0$ 15
 $NA = 0.7$

20

Embodiment 64

25 $R_1 = 1.233$ $R_2 = 6.217$ $D = 1.56$ $n_0 = 1.8$ 25
 $g = 0.458$ $h_4 = -0.791$ $h_6 = -0.991$ $f = 1.0$
 $NA = 0.7$

30

where R_1 , R_2 respectively represent the radii of curvatures of the lens surfaces, D represents the length of the lens, n_0 represents the refractive index on the optical axis of the lens, the parameter g represents the gradient of the refractive index distribution, h_4 and h_6 respectively represent the 4th- and 6th-order coefficients of the refractive index distribution, f represents the focal length of the lens, and NA represents the numerical aperture at the side of the disk. Both the coefficients g of the refractive index distribution and the value of refractive index are for the wave length $\lambda = 780 \text{ nm}$.

Among them, each of Embodiments 52 through 56, 58 through 60 and 62 according to the present invention is a biconvex lens as shown in Fig. 10, and Embodiments 57, 61, 63 and 64 according to the present invention is a positive meniscus lens as shown in Fig. 11.

In Embodiments 1 through 21 of the above mentioned Embodiments according to the present invention, aberrations are corrected for the lens system involving the disk whose thickness and refractive index are 1.2 mm and 1.55 respectively, and in the aberration curves of the respective Embodiments shown as Fig. 12 through 32, the above mentioned disk is taken into account.

In Embodiments 22 through 64 according to the present invention, aberrations are also corrected for the lens system involving the disk whose thickness and refractive index are 0.288 mm and 1.55 respectively, and in the aberration curves of respective Embodiments, the above mentioned disk is also taken into account.

In Embodiments 1 through 64, all of higher-order coefficients than h_6 are regarded as zero.

As is mentioned above, in the GRIN single lens system according to the present invention, N.A. is large and various aberrations including off-axial aberration especially coma are corrected excellently.

55 CLAIMS

1. A graded refractive index single lens system comprising at least one surface formed spherically, having refractive index n expressed by the formula shown below wherein n_0 represents the refractive index on the optical axis of said lens and r represents the radial distance from the optical axis, and satisfying the conditions (1), (2) and (3) shown below:

$$n^2 = n_0^2 [1 - (gr)^2 + h_4(gr)^4 + h_6(gr)^6 + \dots]$$

$$(1) \quad gD < 0.51$$

$$(2) \quad 0.3 < g\phi < 0.7$$

$$(3) \quad 0.28 f < D$$

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where g is a parameter representing the degree of the gradient of the refractive index distribution, h_4 and h_6 respectively represent the 4th- and 6th-order coefficients of said refractive index distribution, D represents the length of said lens, ϕ represents the diameter of said lens and f represents the focal length of said lens.

15 2. A graded refractive index single lens system comprising at least one surface formed spherically, having refractive index n expressed by the formula shown below wherein n_0 represents the refractive index on the optical axis of said lens and r represents the radial distance from the optical axis, and satisfying the conditions (4) and (5) shown below:

$$20 \quad n^2 = n_0^2 [1 - (gr)^2 + h_4(gr)^4 + h_6(gr)^6 + \dots]$$

$$(4) \quad 0.96 f < D < 1.536 f$$

$$25 \quad (5) \quad 0.63 < gf$$

where g is a parameter representing the degree of the gradient of the refractive index distribution, h_4 and h_6 respectively represent the 4th- and 6th-order coefficients of said refractive index distribution, D represents the length of said lens and f represents the focal length of said lens.

30 3. A graded refractive index single lens system comprising at least one surface formed spherically, having refractive index n expressed by the formula shown below wherein n_0 represents the refractive index on the optical axis of said lens and r represents the radial distance from the optical axis, and satisfying the conditions (6), (7) and (8) shown below:

$$35 \quad n^2 = n_0^2 [1 - (gr)^2 + h_4(gr)^4 + h_6(gr)^6 + \dots]$$

$$(6) \quad D < 1.08 f$$

$$40 \quad (7) \quad gf < 0.604$$

$$(8) \quad 0.51 < gD$$

45 where g is a parameter representing the degree of the gradient of the refractive index distribution, h_4 and h_6 respectively represent the 4th- and 6th-order coefficients of said refractive index distribution, D represents the length of said lens and f represents the focal length of said lens.

4. A graded refractive index single lens system comprising at least one surface formed spherically, having refractive index n expressed by the formula shown below wherein n_0 represents the refractive index on the optical axis of said lens and r represents the radial distance from the optical axis, and satisfying the conditions (11), (12) and (13) shown below:

$$n^2 = n_0^2 [1 - (gr)^2 + h_4(gr)^4 + h_6(gr)^6 + \dots]$$

$$55 \quad (11) \quad 1.152 f < D < 1.392 f$$

$$(12) \quad gf < 0.562$$

$$(13) \quad 0.51 < gD$$

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where g is a parameter representing the degree of the gradient of the refractive index distribution, h_4 and h_6 respectively represent the 4th- and 6th-order coefficients of said refractive index distribution, D represents the length of said lens and f represents the focal length of said lens.

5. A graded refractive index single lens system comprising at least one surface formed spherically, having refractive index n expressed by the formula shown below wherein n_0 repre-

sents the refractive index on the optical axis of said lens and r represents the radial distance from the optical axis, and satisfying the conditions (14) and (15) shown below:

$$n^2 = n_0^2 [1 - (gr)^2 + h_4(gr)^4 + h_6(gr)^6 + \dots] \quad 5$$

$$(14) \quad 1.54 f < D$$

$$(15) \quad -4 < (g - 0.5) D \quad 10$$

where g is a parameter representing the degree of the gradient of the refractive index distribution, h_4 and h_6 respectively represent the 4th- and 6th-order coefficients of said refractive index distribution, D represent the length of said lens and f represents the focal length of said lens.

6. A graded refractive index single lens system according to Claim 1 wherein said graded refractive index single lens system has the following numerical data: 15

$$\begin{aligned} R_1 &= 2.847 & R_2 &= \infty & D &= 2.832 & n_0 &= 1.65 \\ g &= 0.12 & h_4 &= 2.404 & h_6 &= 47.99 & \phi &= 3.2 \\ f &= 3.5556 & NA &= 0.45 & WD &= 1.21 & gD &= 0.340 \\ g\phi &= 0.384 & D/f &= 0.796 \end{aligned} \quad 20 \quad 25$$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

7. A graded refractive index single lens system according to Claim 1 wherein said graded refractive index single lens system has the following numerical data: 30

$$\begin{aligned} R_1 &= 3.009 & R_2 &= -62.404 & D &= 3.333 & n_0 &= 1.65 \\ g &= 0.12 & h_4 &= 1.716 & h_6 &= 32.20 & \phi &= 3.2 \\ f &= 3.5556 & NA &= 0.45 & WD &= 0.99 & gD &= 0.400 \\ g\phi &= 0.384 & D/f &= 0.937 \end{aligned} \quad 35 \quad 40$$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

8. A graded refractive index single lens system according to Claim 1 wherein said graded refractive index single lens system has the following numerical data: 45

$$\begin{aligned} R_1 &= 3.194 & R_2 &= -24.832 & D &= 3.750 & n_0 &= 1.65 \\ g &= 0.12 & h_4 &= 1.298 & h_6 &= 23.65 & \phi &= 3.2 \\ f &= 3.5556 & NA &= 0.45 & WD &= 0.84 & gD &= 0.45 \\ g\phi &= 0.384 & D/f &= 1.055 \end{aligned} \quad 50 \quad 55$$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

9. A graded refractive index single lens system according to Claim 1 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 3.458$ $R_2 = -12.852$ $D = 4.167$ $n_0 = 1.65$
 $g = 0.12$ $h_4 = 1.082$ $h_6 = 18.89$ $\phi = 3.2$
5 $f = 3.5556$ $NA = 0.45$ $WD = 0.73$ $gD = 0.5$ 5
 $g\phi = 0.384$ $D/f = 1.172$

10 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 10

10. A graded refractive index single lens system according to Claim 1 wherein said graded refractive index single lens system has the following numerical data:

15 $R_1 = 2.649$ $R_2 = 60.550$ $D = 1.333$ $n_0 = 1.65$ 15
 $g = 0.15$ $h_4 = -0.597$ $h_6 = -2.040$ $\phi = 3.2$
20 $f = 3.5556$ $NA = 0.45$ $WD = 2.01$ $gD = 0.2$ 20
 $g\phi = 0.48$ $D/f = 0.375$

25 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 25

11. A graded refractive index single lens system according to Claim 1 wherein said graded refractive index single lens system has the following numerical data:

30 $R_1 = 2.716$ $R_2 = 40.040$ $D = 1.667$ $n_0 = 1.65$ 30
 $g = 0.15$ $h_4 = -0.611$ $h_6 = -0.923$ $\phi = 3.2$
35 $f = 3.5556$ $NA = 0.45$ $WD = 1.82$ $gD = 0.25$ 35
 $g\phi = 0.48$ $D/f = 0.469$

40 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 40

12. A graded refractive index single lens system according to Claim 1 wherein said graded refractive index single lens system has the following numerical data:

45 $R_1 = 2.792$ $R_2 = 30.725$ $D = 2.0$ $n_0 = 1.65$ 45
 $g = 0.15$ $h_4 = -0.646$ $h_6 = -0.816$ $\phi = 3.2$
 $f = 3.5556$ $NA = 0.45$ $WD = 1.64$ $gD = 0.3$
50 $g\phi = 0.48$ $D/f = 0.562$ 50

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

55 13. A graded refractive index single lens system according to Claim 1 wherein said graded refractive index single lens system has the following numerical data: 55

$R_1 = 2.877$ $R_2 = 25.630$ $D = 2.333$ $n_0 = 1.65$
 $g = 0.15$ $h_4 = -0.691$ $h_6 = -0.993$ $\phi = 3.2$
 $f = 3.5556$ $NA = 0.45$ $WD = 1.45$ $gD = 0.35$
 $g\phi = 0.48$ $D/f = 0.656$

10 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 10

14. A graded refractive index single lens system according to Claim 1 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 2.973$ $R_2 = 22.668$ $D = 2.667$ $n_0 = 1.65$
 $g = 0.15$ $h_4 = -0.735$ $h_6 = -1.227$ $\phi = 3.2$
 $f = 3.5556$ $NA = 0.45$ $WD = 1.28$ $gD = 0.4$
 $g\phi = 0.48$ $D/f = 0.750$

25 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 25

15. A graded refractive index single lens system according to Claim 1 wherein the said graded refractive index single lens system has the following numerical data:

$R_1 = 3.081$ $R_2 = 21.061$ $D = 3.0$ $n_0 = 1.65$
 $g = 0.15$ $h_4 = -0.774$ $h_6 = -1.420$ $\phi = 3.2$
 $f = 3.5556$ $NA = 0.45$ $WD = 1.11$ $gD = 0.45$
 $g\phi = 0.48$ $D/f = 0.844$

40 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 40

16. A graded refractive index single lens system according to Claim 1 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 3.206$ $R_2 = 20.562$ $D = 3.333$ $n_0 = 1.65$
 $g = 0.15$ $h_4 = -0.802$ $h_6 = -1.526$ $\phi = 3.2$
 $f = 3.5556$ $NA = 0.45$ $WD = 0.95$ $gD = 0.5$
 $g\phi = 0.48$ $D/f = 0.937$

50 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 50

55 17. A graded refractive index single lens system according to Claim 1 wherein said graded refractive index single lens system has the following numerical data: 55

$R_1 = 2.916$ $R_2 = 17.811$ $D = 2.059$ $n_0 = 1.65$
 $g = 0.17$ $h_4 = -1.247$ $h_6 = -5.704$ $\phi = 3.2$
5 $f = 3.5556$ $NA = 0.45$ $WD = 1.59$ $gD = 0.35$
 $g\phi = 0.544$ $D/f = 0.579$

10 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 10

18. A graded refractive index single lens system according to Claim 1 wherein said graded refractive index single lens system has the following numerical data:

15 $R_1 = 3.009$ $R_2 = 14.981$ $D = 2.353$ $n_0 = 1.65$
 $g = 0.17$ $h_4 = -1.163$ $h_6 = -4.370$ $\phi = 3.2$
20 $f = 3.5556$ $NA = 0.45$ $WD = 1.44$ $gD = 0.4$
 $g\phi = 0.544$ $D/f = 0.662$

25 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 25

19. A graded refractive index single lens system according to Claim 1 wherein said graded refractive index single lens system has the following numerical data:

30 $R_1 = 3.110$ $R_2 = 12.932$ $D = 2.647$ $n_0 = 1.65$
 $g = 0.17$ $h_4 = -1.099$ $h_6 = -3.524$ $\phi = 3.2$
35 $f = 3.5556$ $NA = 0.45$ $WD = 1.28$ $gD = 0.45$
 $g\phi = 0.544$ $D/f = 0.744$

40 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 40

20. A graded refractive index single lens system according to Claim 1 wherein said graded refractive index single lens system has the following numerical data:

45 $R_1 = 3.219$ $R_2 = 11.371$ $D = 2.941$ $n_0 = 1.65$
 $g = 0.17$ $h_4 = -1.047$ $h_6 = -2.937$ $\phi = 3.2$
 $f = 3.5556$ $NA = 0.45$ $WD = 1.12$ $gD = 0.5$
50 $g\phi = 0.544$ $D/f = 0.827$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

55 21. A graded refractive index single lens system according to Claim 1 wherein said graded refractive index single lens system has the following numerical data: 55

$R_1 = 3.206$ $R_2 = 9.178$ $D = 2.250$ $n_0 = 1.65$
 $g = 0.20$ $h_4 = -1.092$ $h_6 = -2.748$ $\phi = 3.2$
 $f = 3.5556$ $NA = 0.45$ $WD = 1.48$ $gD = 0.45$
 $g\phi = 0.64$ $D/f = 0.633$

10 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 10

22. A graded refractive index single lens system according to Claim 1 wherein said graded refractive index single lens system has the following numerical data:

15 $R_1 = 3.318$ $R_2 = 7.883$ $D = 2.5$ $n_0 = 1.65$ 15
 $g = 0.20$ $h_4 = -0.986$ $h_6 = -2.099$ $\phi = 3.2$
20 $f = 3.5556$ $NA = 0.45$ $WD = 1.34$ $gD = 0.5$ 20
 $g\phi = 0.64$ $D/f = 0.703$

25 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 25

23. A graded refractive index single lens system according to Claim 1 wherein said graded refractive index single lens system has the following numerical data:

30 $R_1 = 3.148$ $R_2 = 65.733$ $D = 3.5$ $n_0 = 1.7$ 30
 $g = 0.12$ $h_4 = 0.909$ $h_6 = 19.14$ $\phi = 3.2$
35 $f = 3.5556$ $NA = 0.45$ $WD = 0.89$ $gD = 0.42$ 35
 $g\phi = 0.384$ $D/f = 0.984$

40 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 40

24. A graded refractive index single lens system according to Claim 1 wherein said graded refractive index single lens system has the following numerical data:

45 $R_1 = 3.149$ $R_2 = 10.286$ $D = 2.5$ $n_0 = 1.7$ 45
 $g = 0.17$ $h_4 = -1.169$ $h_6 = -3.832$ $\phi = 3.2$
 $f = 3.5556$ $NA = 0.45$ $WD = 1.34$ $gD = 0.425$
50 $g\phi = 0.544$ $D/f = 0.703$ 50

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

55 25. A graded refractive index single lens system according to Claim 1 wherein said graded refractive index single lens system has the following numerical data: 55

$R_1 = 2.760$ $R_2 = -14.835$ $D = 3.0$ $n_0 = 1.55$
 $g = 0.13$ $h_4 = 1.839$ $h_6 = 36.50$ $\phi = 3.2$
5 $f = 3.5556$ $NA = 0.45$ $WD = 1.18$ $gD = 0.39$ 5
 $g\phi = 0.416$ $D/f = 0.844$

10 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 10

26. A graded refractive index single lens system according to Claim 1 wherein said graded refractive index single lens system has the following numerical data:

15 $R_1 = 2.512$ $R_2 = -43.624$ $D = 1.5$ $n_0 = 1.55$ 15
 $g = 0.16$ $h_4 = -0.608$ $h_6 = -2.217$ $\phi = 3.2$
20 $f = 3.5556$ $NA = 0.45$ $WD = 1.93$ $gD = 0.24$ 20
 $g\phi = 0.512$ $D/f = 0.422$

25 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 25

27. A graded refractive index single lens system according to Claim 2 wherein said graded refractive index single lens system has the following numerical data:

30 $R_1 = 1.234$ $R_2 = 7.004$ $D = 1.440$ $n_0 = 1.50$ 30
 $g = 0.646$ $h_4 = -0.500$ $h_6 = -0.426$ $f = 1.0$
35 $NA = 0.5$ 35

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

40 28. A graded refractive index single lens system according to Claim 2 wherein said graded refractive index single lens system has the following numerical data: 40

$R_1 = 1.013$ $R_2 = 4.115$ $D = 1.140$ $n_0 = 1.50$
45 $g = 0.667$ $h_4 = -0.718$ $h_6 = -1.144$ $f = 1.0$ 45
 $NA = 0.5$

50 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 50

29. A graded refractive index single lens system according to Claim 2 wherein said graded refractive index single lens system has the following numerical data:

55 $R_1 = 1.167$ $R_2 = 1.230$ $D = 1.320$ $n_0 = 1.50$ 55
 $g = 0.708$ $h_4 = -0.530$ $h_6 = -0.501$ $f = 1.0$
 $NA = 0.5$

60 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 60

30. A graded refractive index single lens system according to Claim 2 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 1.039$ $R_2 = 1.719$ $D = 1.080$ $n_0 = 1.50$
 $g = 0.729$ $h_4 = -0.640$ $h_6 = -0.809$ $f = 1.0$
 5 $NA = 0.5$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

31. A graded refractive index single lens system according to Claim 2 wherein said graded refractive index single lens system has the following numerical data:

15 $R_1 = 1.190$ $R_2 = 0.699$ $D = 1.200$ $n_0 = 1.50$
 $g = 0.792$ $h_4 = -0.385$ $h_6 = -0.221$ $f = 1.0$
 20 $NA = 0.5$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

32. A graded refractive index single lens system according to Claim 2 wherein said graded refractive index single lens system has the following numerical data:

25 $R_1 = 1.025$ $R_2 = 1.462$ $D = 1.080$ $n_0 = 1.65$
 $g = 0.646$ $h_4 = -0.847$ $h_6 = -1.547$ $f = 1.0$
 30 $NA = 0.5$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

33. A graded refractive index single lens system according to Claim 2 wherein said graded refractive index single lens system has the following numerical data:

40 $R_1 = 1.244$ $R_2 = 0.630$ $D = 1.368$ $n_0 = 1.65$
 $g = 0.688$ $h_4 = -0.533$ $h_6 = -0.501$ $f = 1.0$
 45 $NA = 0.5$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

34. A graded refractive index single lens system according to Claim 2 wherein said graded refractive index single lens system has the following numerical data:

50 $R_1 = 1.117$ $R_2 = 0.874$ $D = 1.140$ $n_0 = 1.65$
 $g = 0.708$ $h_4 = -0.628$ $h_6 = -0.719$ $f = 1.0$
 55 $NA = 0.5$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

35. A graded refractive index single lens system according to Claim 2 wherein said graded refractive index single lens system has the following numerical data:

60 $NA = 0.5$

$$\begin{array}{llll}
 R_1 = 1.103 & R_2 = 0.902 & D = 1.020 & n_0 = 1.65 \\
 g = 0.750 & h_4 = -0.570 & h_6 = -0.568 & f = 1.0 \\
 5 \quad NA = 0.5 & & &
 \end{array}$$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

36. A graded refractive index single lens system according to Claim 2 wherein said graded refractive index single lens system has the following numerical data:

$$\begin{array}{llll}
 15 \quad R_1 = 1.231 & R_2 = 2.313 & D = 1.440 & n_0 = 1.50 \\
 g = 0.667 & h_4 = -0.510 & h_6 = -0.489 & f = 1.0 \\
 NA = 0.6 & & &
 \end{array}$$

20 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

37. A graded refractive index single lens system according to Claim 2 wherein said graded refractive index single lens system has the following numerical data:

$$\begin{array}{llll}
 25 \quad R_1 = 1.213 & R_2 = 1.065 & D = 1.380 & n_0 = 1.50 \\
 g = 0.708 & h_4 = -0.488 & h_6 = -0.432 & f = 1.0 \\
 30 \quad NA = 0.6 & & &
 \end{array}$$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

35 38. A graded refractive index single lens system according to Claim 3, further satisfying the conditions (9), (10) shown below:

$$\begin{array}{l}
 (9) \quad 2 < |R_2/R_1| \\
 40 \quad (10) \quad h_4 < 0
 \end{array}$$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

45 39. A graded refractive index single lens system according to Claim 38 wherein said graded refractive index single lens system has the following numerical data:

$$\begin{array}{llll}
 R_1 = 0.866 & R_2 = -4.095 & D = 1.02 & n_0 = 1.5 \\
 50 \quad g = 0.563 & h_4 = -0.468 & h_6 = 0.822 & f = 1.0 \\
 NA = 0.5 & WD = 0.283 & &
 \end{array}$$

55 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

40. A graded refractive index single lens system according to Claim 38 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 0.815$ $R_2 = -9.840$ $D = 0.876$ $n_0 = 1.5$
 $g = 0.592$ $h_4 = -0.704$ $h_6 = -1.402$ $f = 1.0$
 $NA = 0.5$ $WD = 0.340$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

41. A graded refractive index single lens system according to Claim 38 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 0.903$ $R_2 = 5.311$ $D = 1.010$ $n_0 = 1.65$
 $g = 0.521$ $h_4 = -0.699$ $h_6 = -0.666$ $f = 1.0$
 $NA = 0.5$ $WD = 0.259$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

42. A graded refractive index single lens system according to Claim 38 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 0.966$ $R_2 = 2.452$ $D = 1.060$ $n_0 = 1.65$
 $g = 0.585$ $h_4 = -0.936$ $h_6 = -2.223$ $f = 1.0$
 $NA = 0.5$ $WD = 0.223$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

43. A graded refractive index single lens system according to Claim 38 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 0.905$ $R_2 = 20.534$ $D = 1.070$ $n_0 = 1.65$
 $g = 0.479$ $h_4 = -0.210$ $h_6 = 4.469$ $f = 1.0$
 $NA = 0.5$ $WD = 0.240$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

44. A graded refractive index single lens system according to Claim 38 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 0.932$ $R_2 = 3.942$ $D = 1.050$ $n_0 = 1.65$
 $g = 0.542$ $h_4 = -0.846$ $h_6 = -1.904$ $f = 1.0$
 $NA = 0.55$ $WD = 0.237$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

45. A graded refractive index single lens system according to Claim 38 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 0.891$ $R_2 = 3.727$ $D = 0.924$ $n_0 = 1.65$
 $g = 0.554$ $h_4 = -0.886$ $h_6 = -2.415$ $f = 1.0$
 5 $NA = 0.55$ $WD = 0.295$ 5

10 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

46. A graded refractive index single lens system according to Claim 38 wherein said graded refractive index single lens system has the following numerical data:

15 $R_1 = 0.871$ $R_2 = -6.682$ $D = 1.020$ $n_0 = 1.5$
 $g = 0.583$ $h_4 = -0.657$ $h_6 = -0.832$ $f = 1.0$
 $NA = 0.6$ $WD = 0.275$ 15

20 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

47. A graded refractive index single lens system according to Claim 38 wherein said graded refractive index single lens system has the following numerical data:

25 $R_1 = 0.816$ $R_2 = -8.201$ $D = 0.900$ $n_0 = 1.5$
 $g = 0.583$ $h_4 = -0.649$ $h_6 = -0.860$ $f = 1.0$
 30 $NA = 0.6$ $WD = 0.329$ 30

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

35 48. A graded refractive index single lens system according to Claim 38 wherein said graded refractive index single lens system has the following numerical data:

40 $R_1 = 0.915$ $R_2 = 7.404$ $D = 1.070$ $n_0 = 1.65$
 $g = 0.504$ $h_4 = -0.579$ $h_6 = 0.942$ $f = 1.0$
 $NA = 0.6$ $WD = 0.234$ 40

45 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

49. A graded refractive index single lens system according to Claim 4 wherein said graded refractive index single lens system has the following numerical data:

50 $R_1 = 1.075$ $R_2 = 16.903$ $D = 1.320$ $n_0 = 1.65$
 $g = 0.521$ $h_4 = -0.693$ $h_6 = -0.677$ $f = 1.0$

55 $NA = 0.5$ 55

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

50. A graded refractive index single lens system according to Claim 4 wherein said graded refractive index single lens system has the following numerical data:

60

$R_1 = 1.069$ $R_2 = -15.880$ $D = 1.368$ $n_0 = 1.80$
 $g = 0.375$ $h_4 = 1.058$ $h_6 = 21.635$ $f = 1.0$
 5 $NA = 0.5$ 5

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 10

51. A graded refractive index single lens system according to Claim 4 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 1.035$ $R_2 = 2.0750$ $D = 1.248$ $n_0 = 1.80$
 $g = 0.479$ $h_4 = -0.954$ $h_6 = -2.156$ $f = 1.0$
 15 $NA = 0.5$ 15

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 20

52. A graded refractive index single lens system according to Claim 4 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 1.022$ $R_2 = 115.424$ $D = 1.272$ $n_0 = 1.65$
 $g = 0.500$ $h_4 = -0.602$ $h_6 = 0.441$ $f = 1.0$
 25 $NA = 0.6$ 30

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

53. A graded refractive index single lens system according to Claim 4 wherein said graded refractive index single lens system has the following numerical data: 35

$R_1 = 1.002$ $R_2 = 4.042$ $D = 1.200$ $n_0 = 1.65$
 $g = 0.542$ $h_4 = -0.844$ $h_6 = -1.800$ $f = 1.0$
 40 $NA = 0.6$ 40

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 45

54. A graded refractive index single lens system according to Claim 4 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 1.039$ $R_2 = 5.178$ $D = 1.320$ $n_0 = 1.80$
 $g = 0.417$ $h_4 = -0.296$ $h_6 = 5.302$ $f = 1.0$
 50 $NA = 0.6$ 55

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

55. A graded refractive index single lens system according to Claim 4 wherein said graded refractive index single lens system has the following numerical data: 60

$R_1 = 1.059$ $R_2 = 2.671$ $D = 1.320$ $n_0 = 1.80$
 $g = 0.458$ $h_4 = -0.854$ $h_6 = -1.367$ $f = 1.0$
 $NA = 0.6$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

56. A graded refractive index single lens system according to Claim 4 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 1.060$ $R_2 = 10.703$ $D = 1.320$ $n_0 = 1.65$
 $g = 0.521$ $h_4 = -0.741$ $h_6 = -0.911$ $f = 1.0$
 $NA = 0.65$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

57. A graded refractive index single lens system according to Claim 4 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 1.074$ $R_2 = 3.970$ $D = 1.368$ $n_0 = 1.80$
 $g = 0.438$ $h_4 = -0.682$ $h_6 = -0.661$ $f = 1.0$
 $NA = 0.65$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

58. A graded refractive index single lens system according to Claim 5 wherein said graded refractive index single lens system has the following data:

$R_1 = 1.697$ $R_2 = -1.356$ $D = 1.56$ $n_0 = 1.5$
 $g = 0.583$ $h_4 = 0.208$ $h_6 = 1.640$ $f = 1.0$
 $NA = 0.5$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

59. A graded refractive index single lens system according to Claim 5 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 1.830$ $R_2 = -1.518$ $D = 1.68$ $n_0 = 1.65$
 $g = 0.500$ $h_4 = 0.530$ $h_6 = 3.966$ $f = 1.0$
 $NA = 0.5$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

60. A graded refractive index single lens system according to Claim 5 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 2.195$ $R_2 = -1.807$ $D = 1.92$ $n_0 = 1.65$
 $g = 0.542$ $h_4 = 0.120$ $h_6 = 0.561$ $f = 1.0$
 5 $NA = 0.5$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface. 10

61. A graded refractive index single lens system according to Claim 5 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 1.332$ $R_2 = -2.166$ $D = 1.56$ $n_0 = 1.8$
 15 $g = 0.375$ $h_4 = 1.755$ $h_6 = 26.713$ $f = 1.0$
 $NA = 0.5$

20 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

62. A graded refractive index single lens system according to Claim 5 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 1.657$ $R_2 = -3.000$ $D = 1.80$ $n_0 = 1.8$
 25 $g = 0.458$ $h_4 = -0.103$ $h_6 = 1.743$ $f = 1.0$
 30 $NA = 0.5$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

35 63. A graded refractive index single lens system according to Claim 5 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 1.355$ $R_2 = 1.906$ $D = 1.56$ $n_0 = 1.5$
 40 $g = 0.667$ $h_4 = -0.415$ $h_6 = -0.316$ $f = 1.0$
 $NA = 0.6$

45 where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

64. A graded refractive index single lens system according to Claim 5 wherein said graded refractive index single lens system has the following numerical data:

$R_1 = 1.500$ $R_2 = -4.096$ $D = 1.62$ $n_0 = 1.5$
 50 $g = 0.625$ $h_4 = -0.268$ $h_6 = 0.024$ $f = 1.0$
 55 $NA = 0.6$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

60 65. A graded refractive index single lens system according to Claim 5 wherein said graded refractive index single lens system has the following numerical data:

$$\begin{array}{llll}
 R_1 = 1.303 & R_2 = -374.044 & D = 1.56 & n_0 = 1.65 \\
 g = 0.542 & h_4 = -0.570 & h_6 = -0.430 & f = 1.0 \\
 NA = 0.6
 \end{array}$$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

66. A graded refractive index single lens system according to Claim 5 wherein said graded refractive index single lens system has the following numerical data:

$$\begin{array}{llll}
 R_1 = 1.771 & R_2 = -2.650 & D = 1.80 & n_0 = 1.65 \\
 g = 0.542 & h_4 = -0.130 & h_6 = 0.446 & f = 1.0 \\
 NA = 0.6
 \end{array}$$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

67. A graded refractive index single lens system according to Claim 5 wherein said graded refractive index single lens system has the following numerical data:

$$\begin{array}{llll}
 R_1 = 1.389 & R_2 = 2.792 & D = 1.68 & n_0 = 1.8 \\
 g = 0.500 & h_4 = -0.747 & h_6 = -1.277 & f = 1.0 \\
 NA = 0.6
 \end{array}$$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

68. A graded refractive index single lens system according to Claim 5 wherein said graded refractive index single lens system has the following numerical data:

$$\begin{array}{llll}
 R_1 = 1.322 & R_2 = -7.400 & D = 1.62 & n_0 = 1.8 \\
 g = 0.438 & h_4 = -0.410 & h_6 = 1.969 & f = 1.0 \\
 NA = 0.6
 \end{array}$$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

69. A graded refractive index single lens system according to Claim 5 wherein said graded refractive index single lens system has the following numerical data:

$$\begin{array}{llll}
 R_1 = 1.289 & R_2 = 47.625 & D = 1.56 & n_0 = 1.65 \\
 g = 0.542 & h_4 = -0.601 & h_6 = -0.530 & f = 1.0 \\
 NA = 0.7
 \end{array}$$

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and the exit side surface.

70. A graded refractive index single lens system according to Claim 5 wherein said graded refractive index single lens system has the following numerical data:

$$R_1 = 1.233$$

$$R_2 = 6.217$$

$$D = 1.56$$

$$n_0 = 1.8$$

$$g = 0.458$$

$$h_4 = -0.791$$

$$h_6 = -0.991$$

$$f = 1.0$$

$$^5 \text{ NA} = 0.7$$

5

where R_1 and R_2 respectively represent the radii of curvatures of the incident side surface and
10 the exit side surface.

10

71. A graded refractive index single lens system substantially as hereinbefore described with reference to and as shown in the accompanying drawings.

72. A graded refractive index single lens system substantially as hereinbefore described according to any one of the embodiments.